

Bayesian statistics approach to interferometry

RESOLVE meets ALMA

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Observational astrophysics 101



Image credit: NASA, ESA, CSA, and STScI

Observational astrophysics 101

$$R = 1.22 \frac{\lambda}{D}$$

$$R = 0.2'' = 500 \text{ au @ 8000 light years}$$

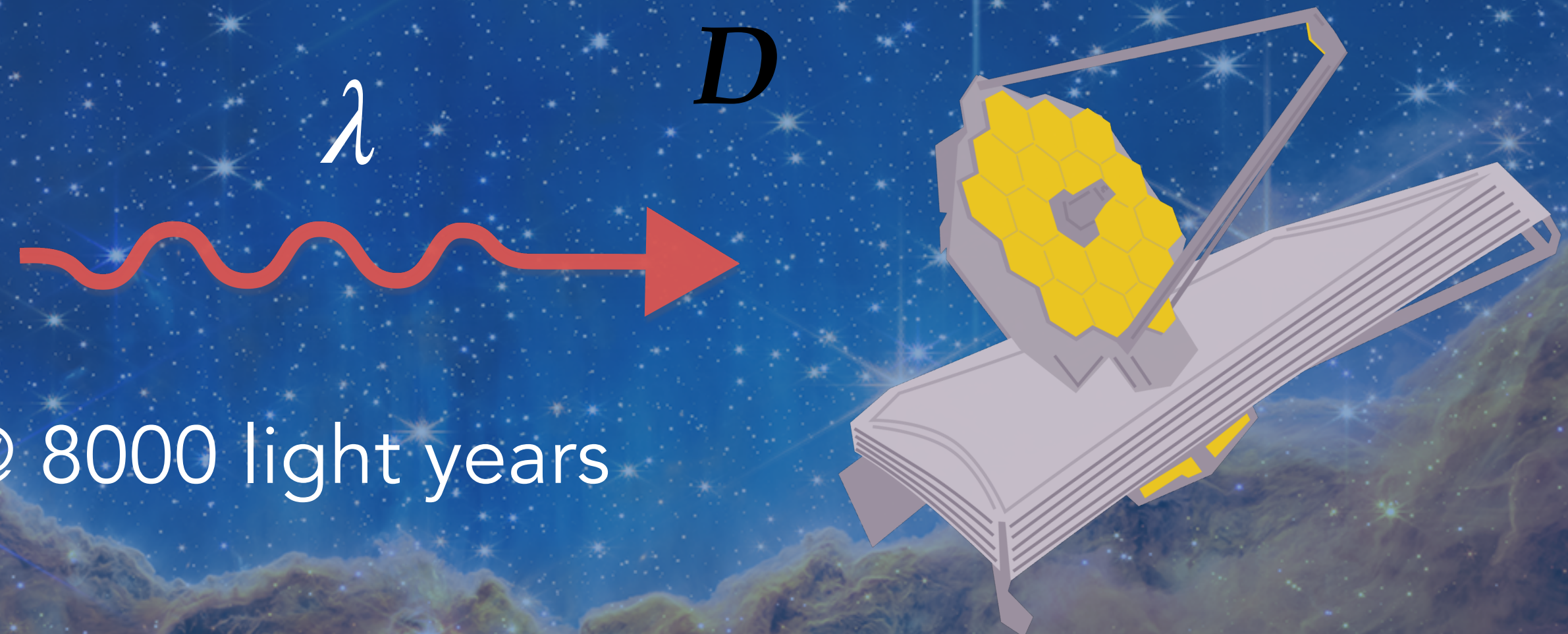


Image credit: NASA, ESA, CSA, and STScI

Longer wavelengths: peering into the cooler universe



Image credit: NASA, ESA, CSA, and STScI

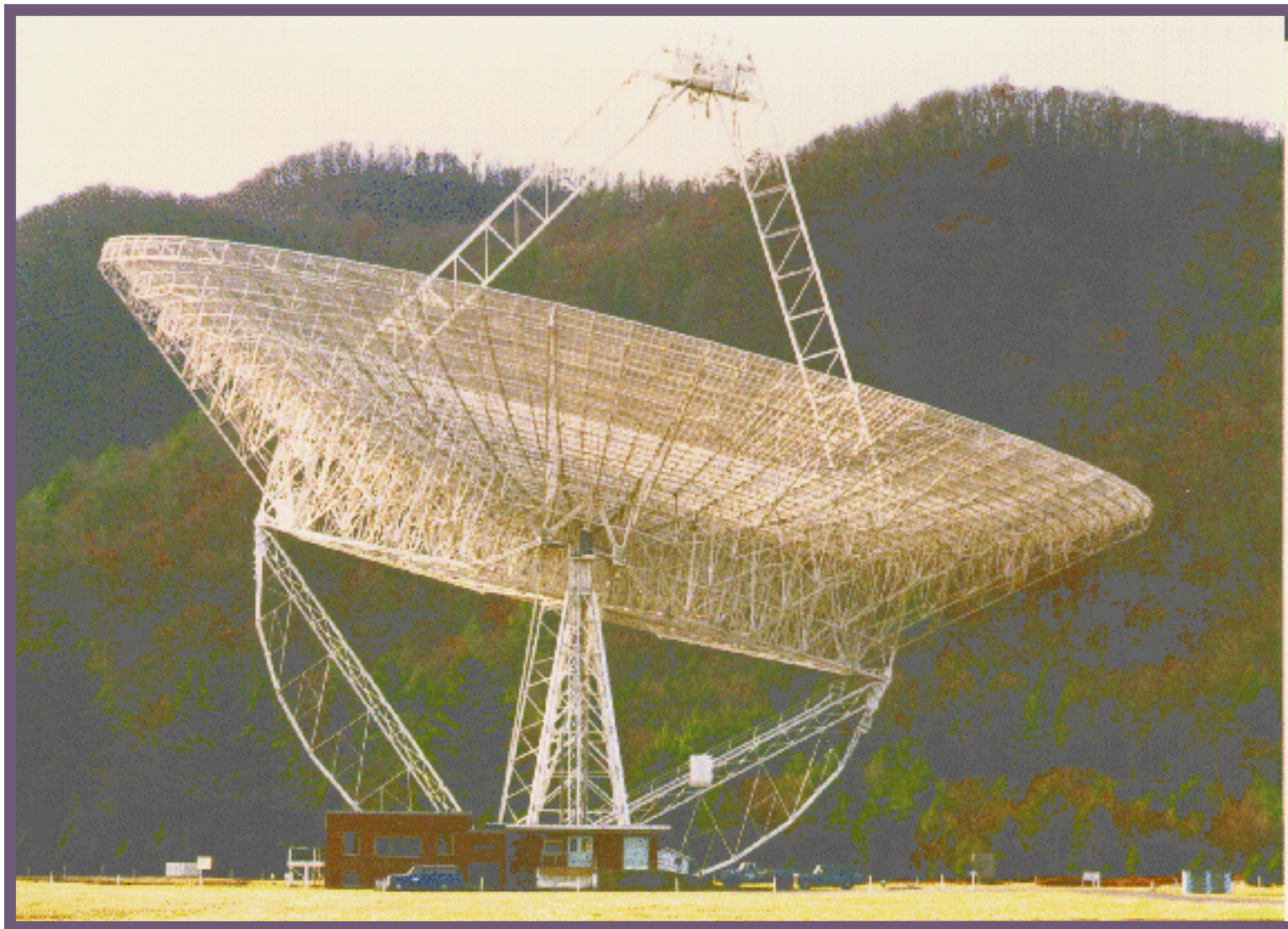
Longer wavelengths: peering into the cooler universe



Image credit: NASA, ESA, CSA, and STScI

For longer wavelengths we need bigger telescopes...

Old Green Bank Telescope (90 m)



$$R = 1.22 \frac{\lambda}{D}$$

$$R = 30'' = 80\,000 \text{ au @ } 8000 \text{ light years}$$

Image credit: Richard Porcas/NRAO

For longer wavelengths we need bigger telescopes...



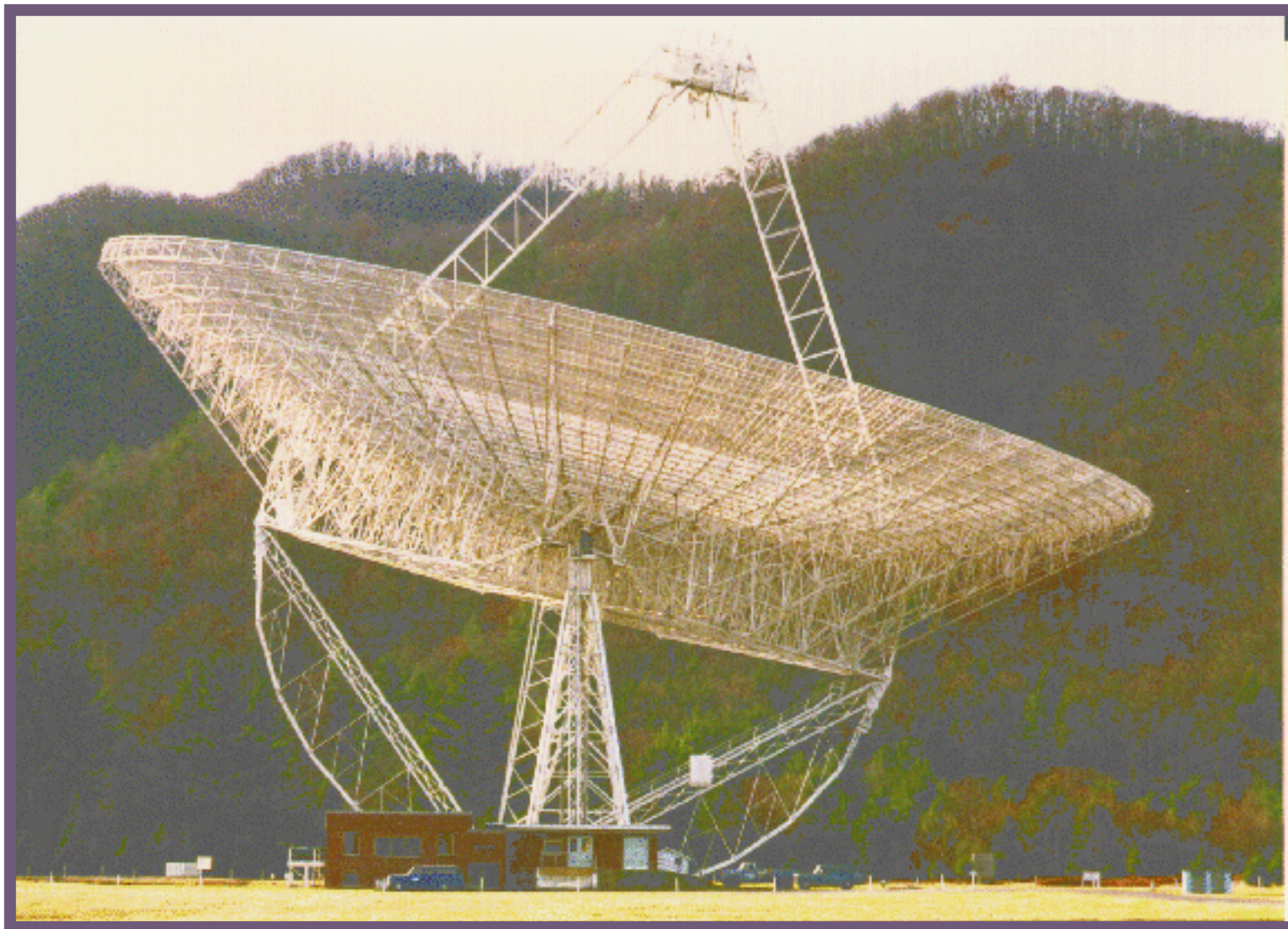
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...and building big telescopes is hard!

Old Green Bank Telescope (0 m)



Image credit: Richard Porcas/NRAO

...and building big telescopes is hard!

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Image credit: Richard Porcas/NRAO

Very Large Array (25 m)

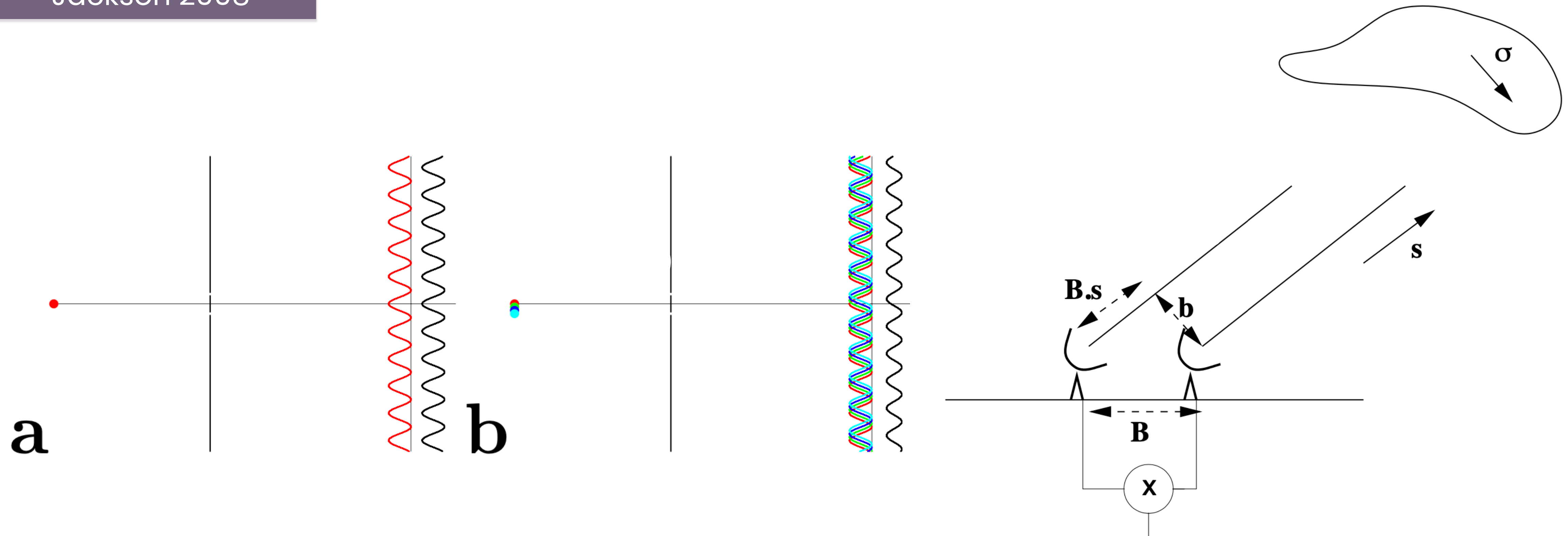


Image credit: NRAO

We can use many small telescopes as one big array!

Young experiment - principle of interferometry

Jackson 2008



Interferometry - using wave properties of light to overcome technical limitations

Atacama Large Millimeter/submillimeter Array (ALMA)

5000 m.a.s.l at Atacama Plateau – one of the driest places on Earth

66 antennas (12 and 7 metres diameter)

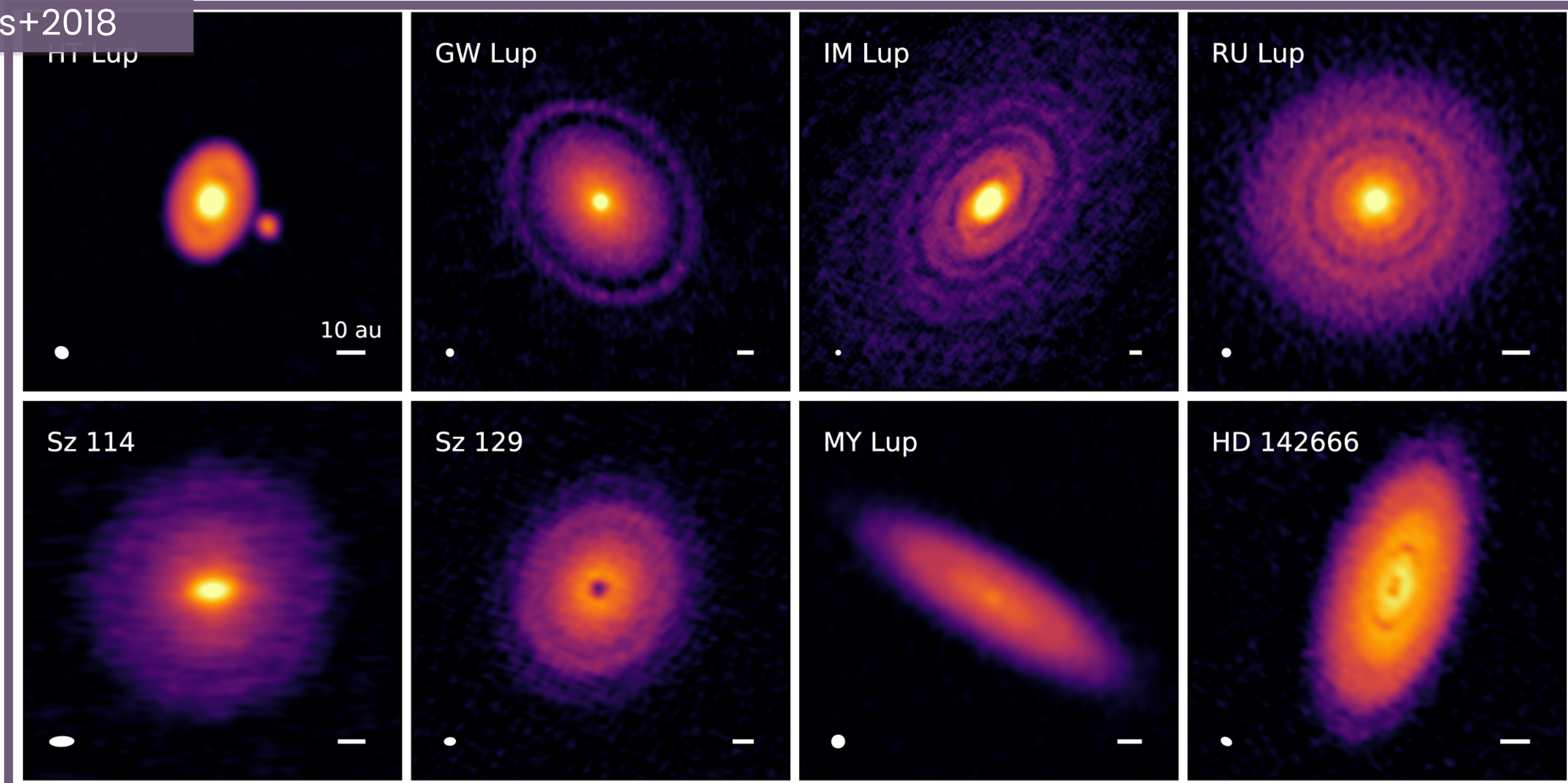
Configurations from 160 m to 16 km max. baseline



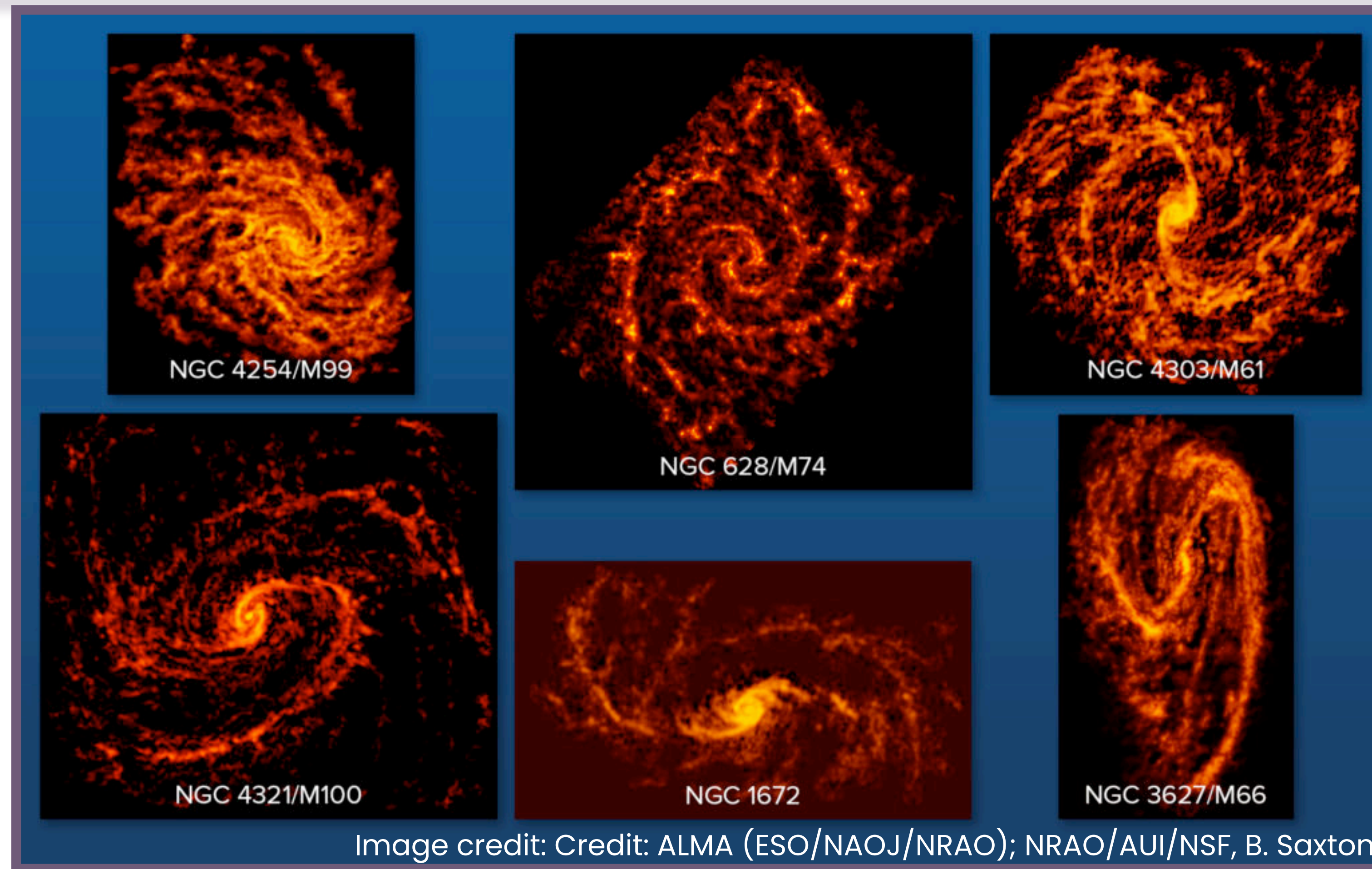
Image credit: ALMA

Revolution of interferometry – ALMA

Andrews+2018



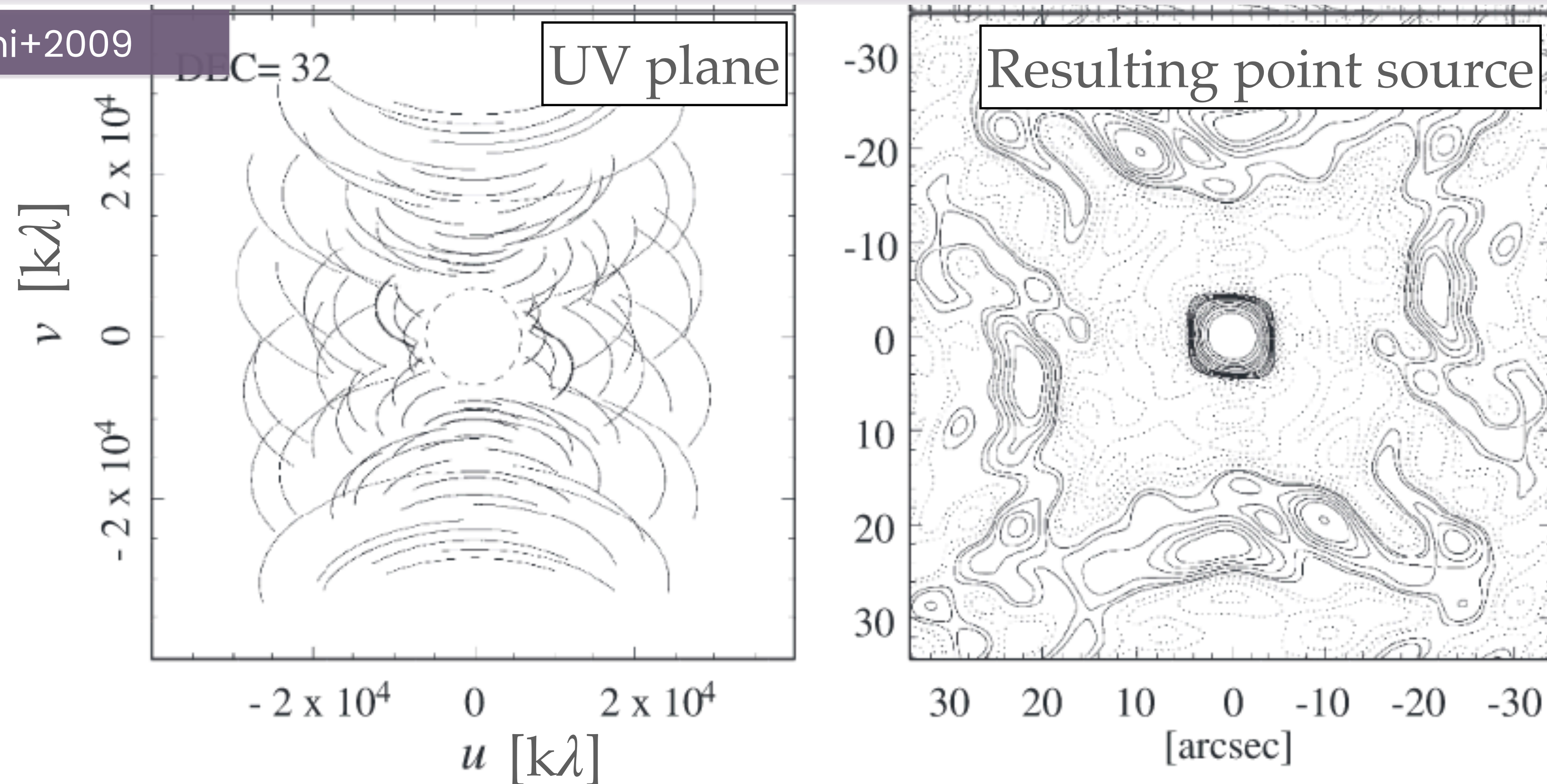
Revolution of interferometry – ALMA



ALMA delivered stunning images at various cosmic scales

Missing information problem in interferometry

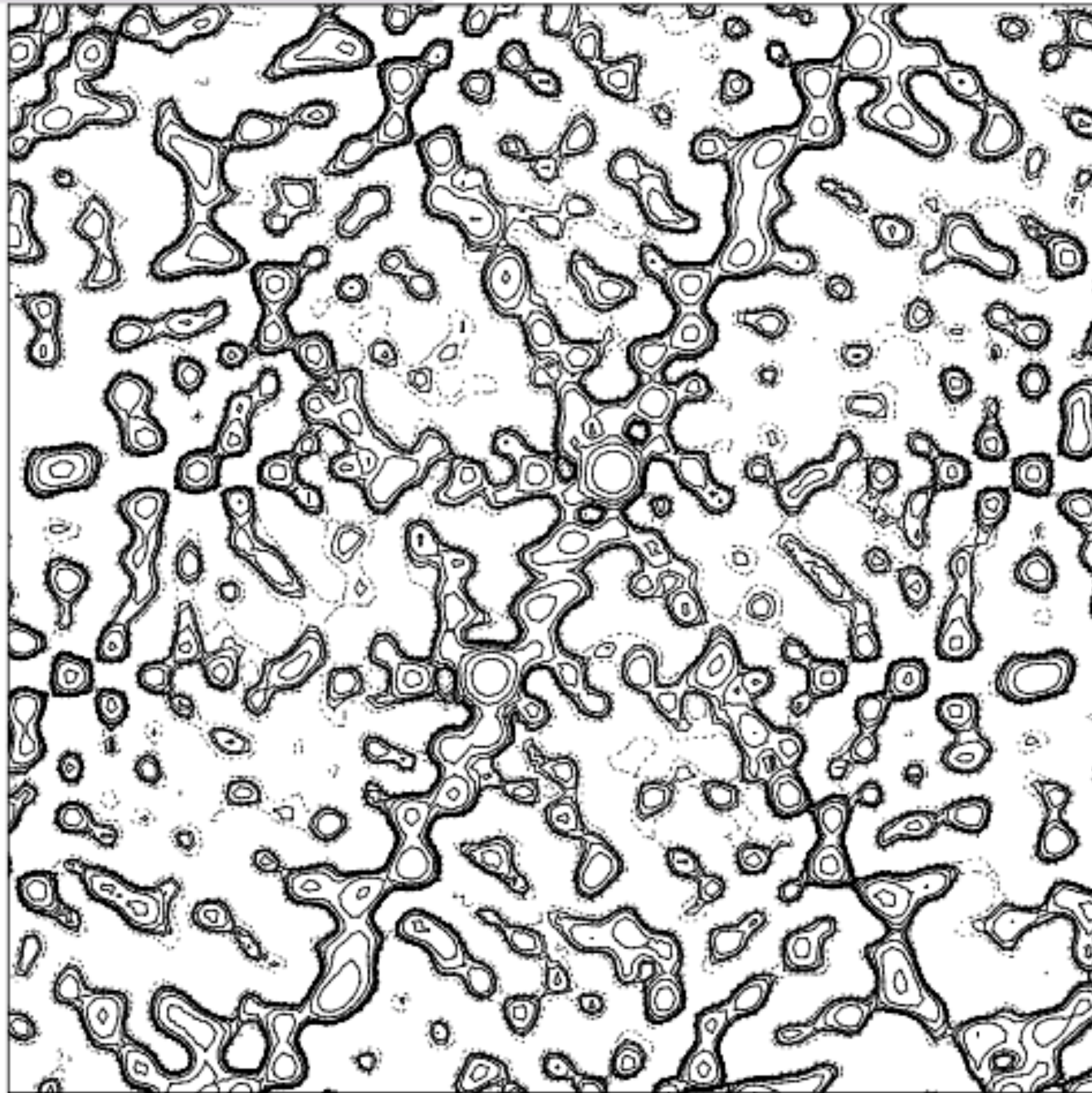
Iguchi+2009



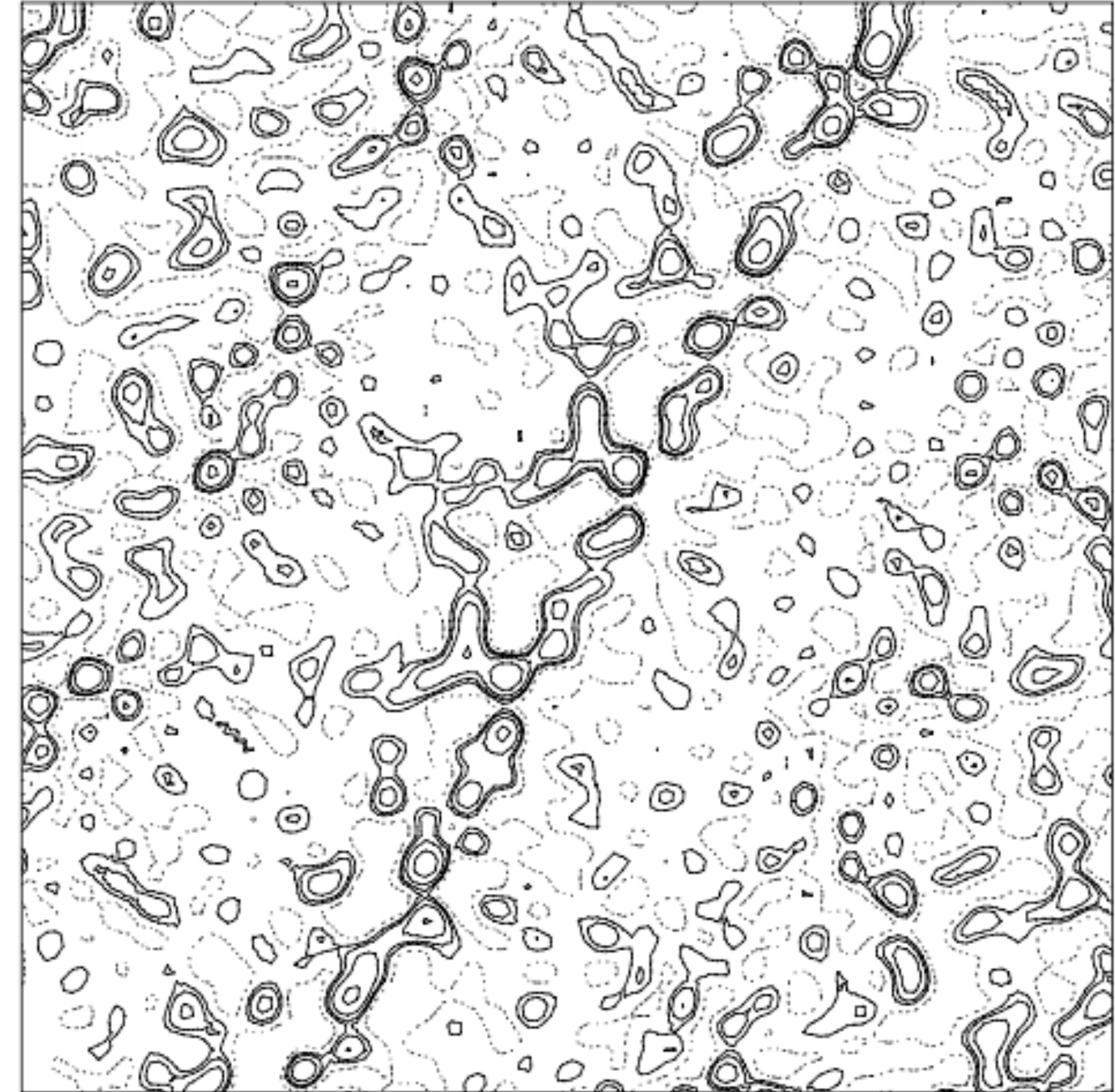
Superior resolution comes with a cost - we cannot sample all scales equally

CLEAN fundamentals

Jackson 2008

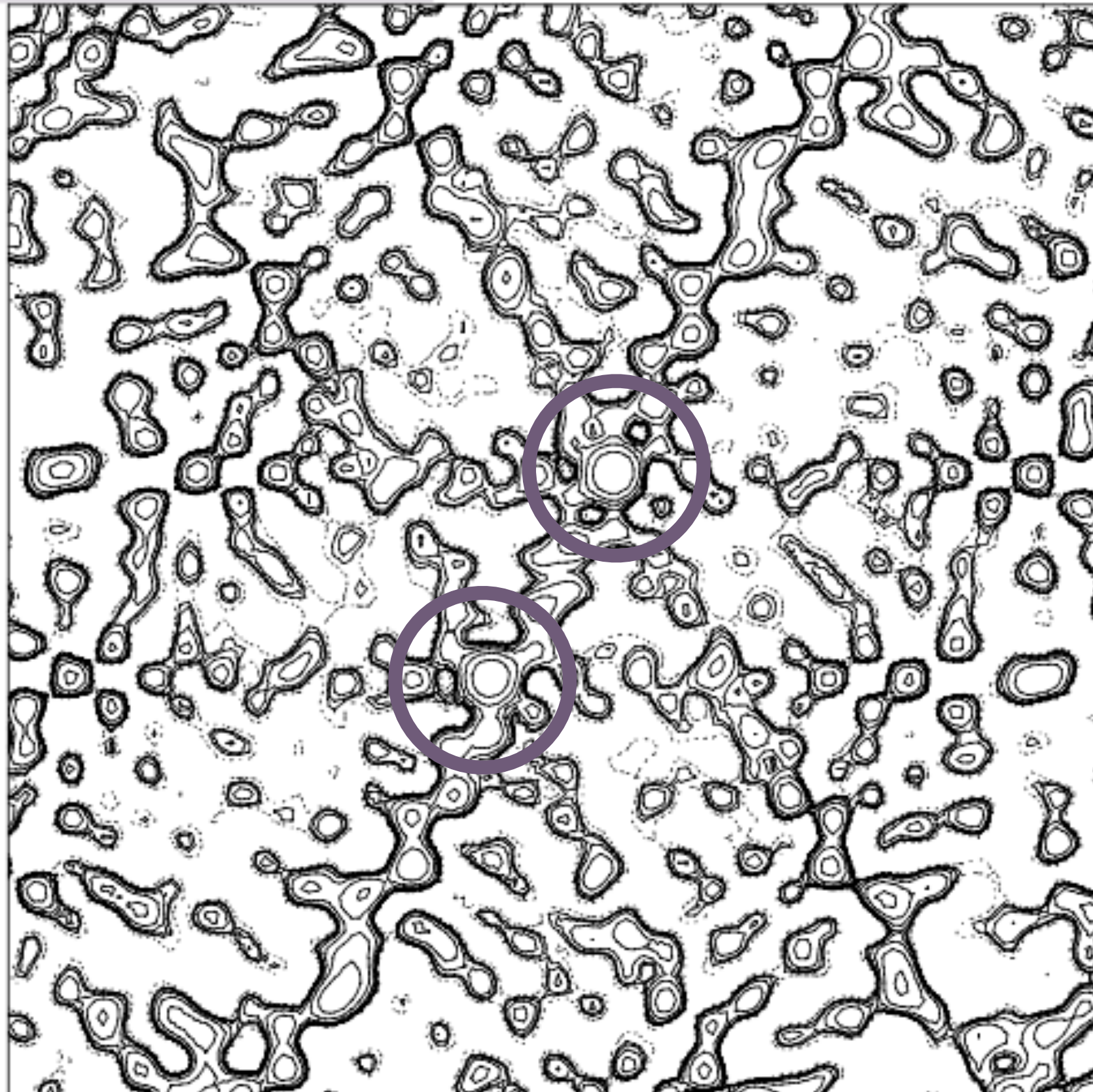


*remove
PSF*

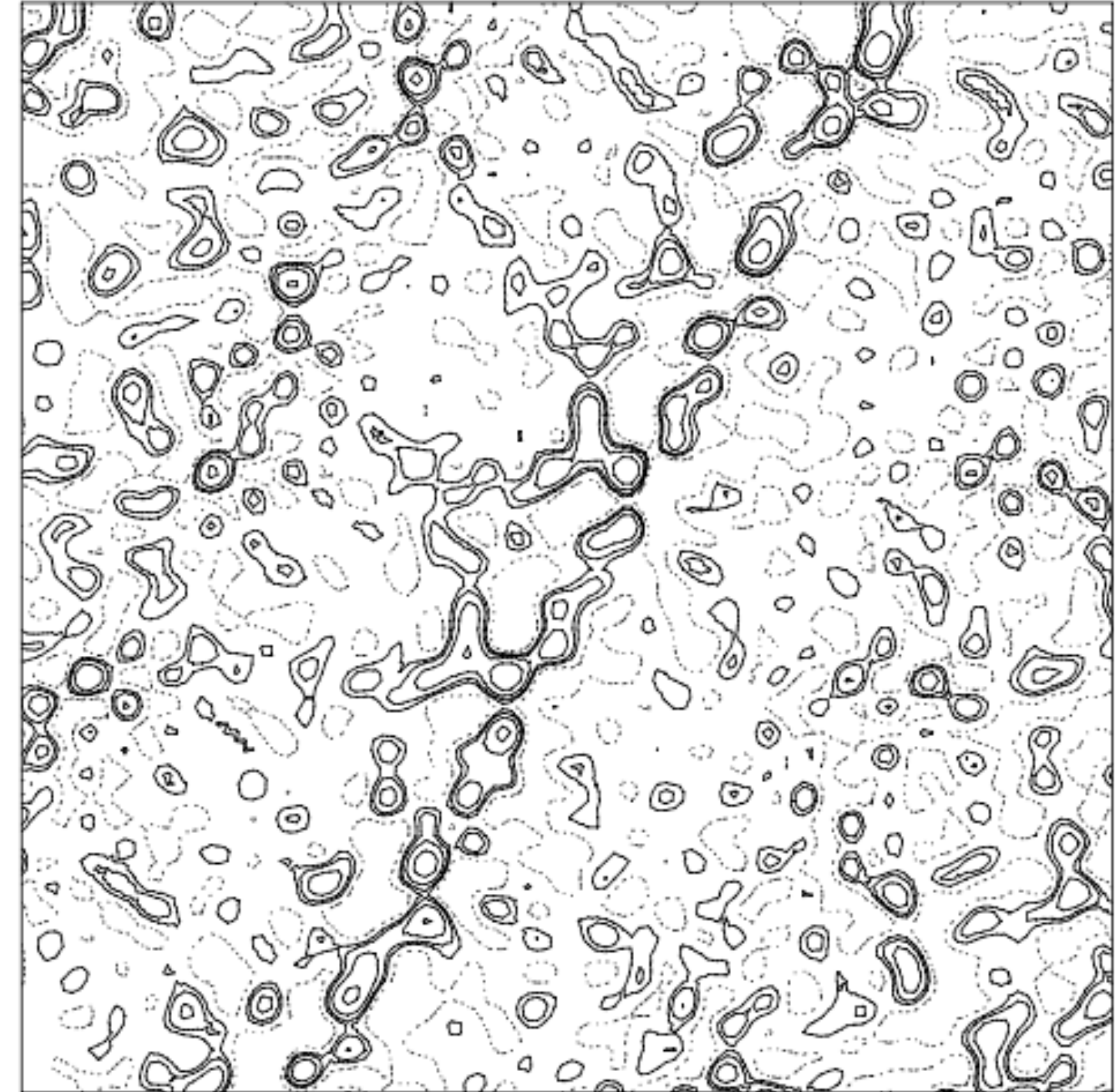


CLEAN fundamentals

Jackson 2008

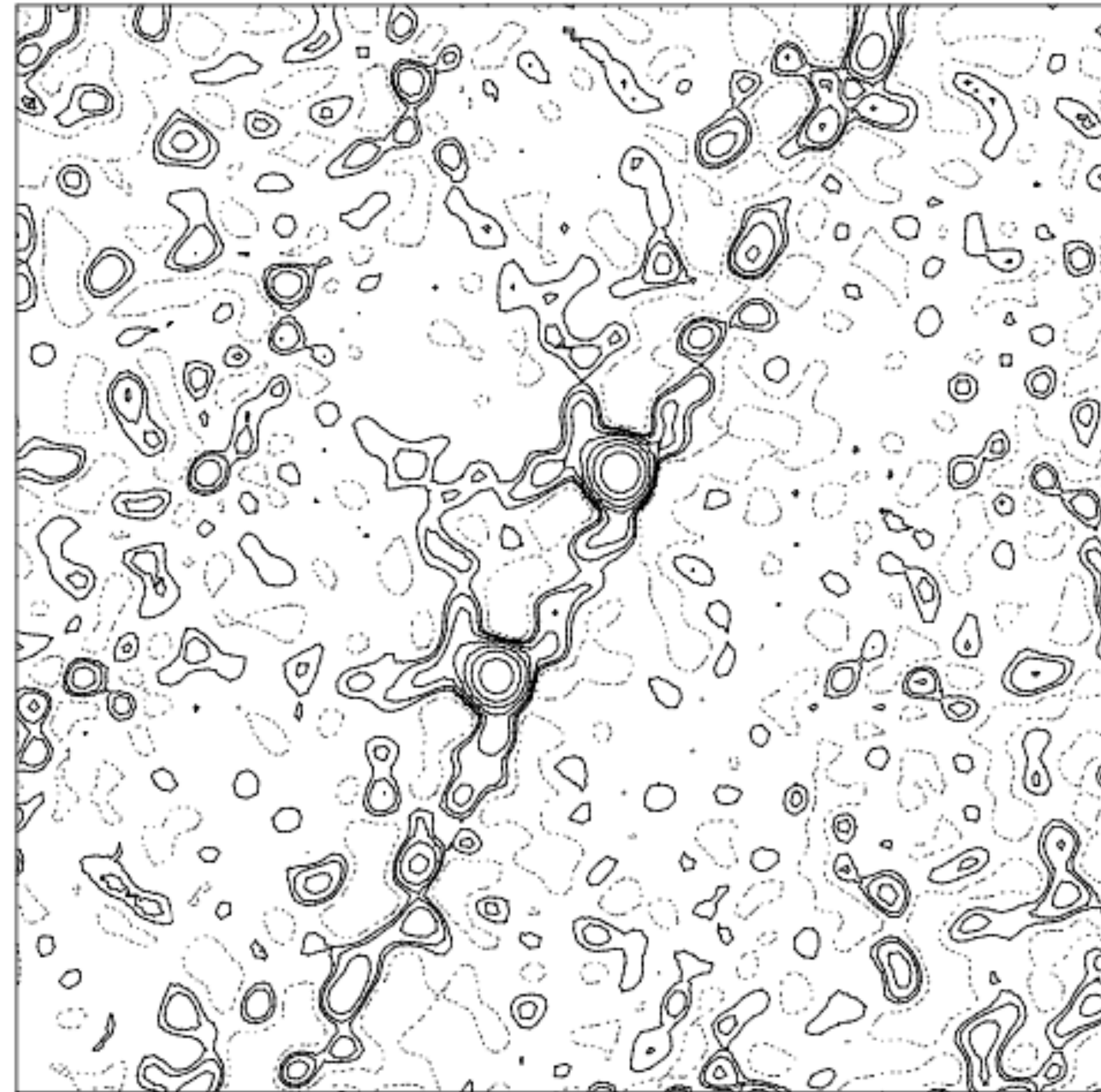
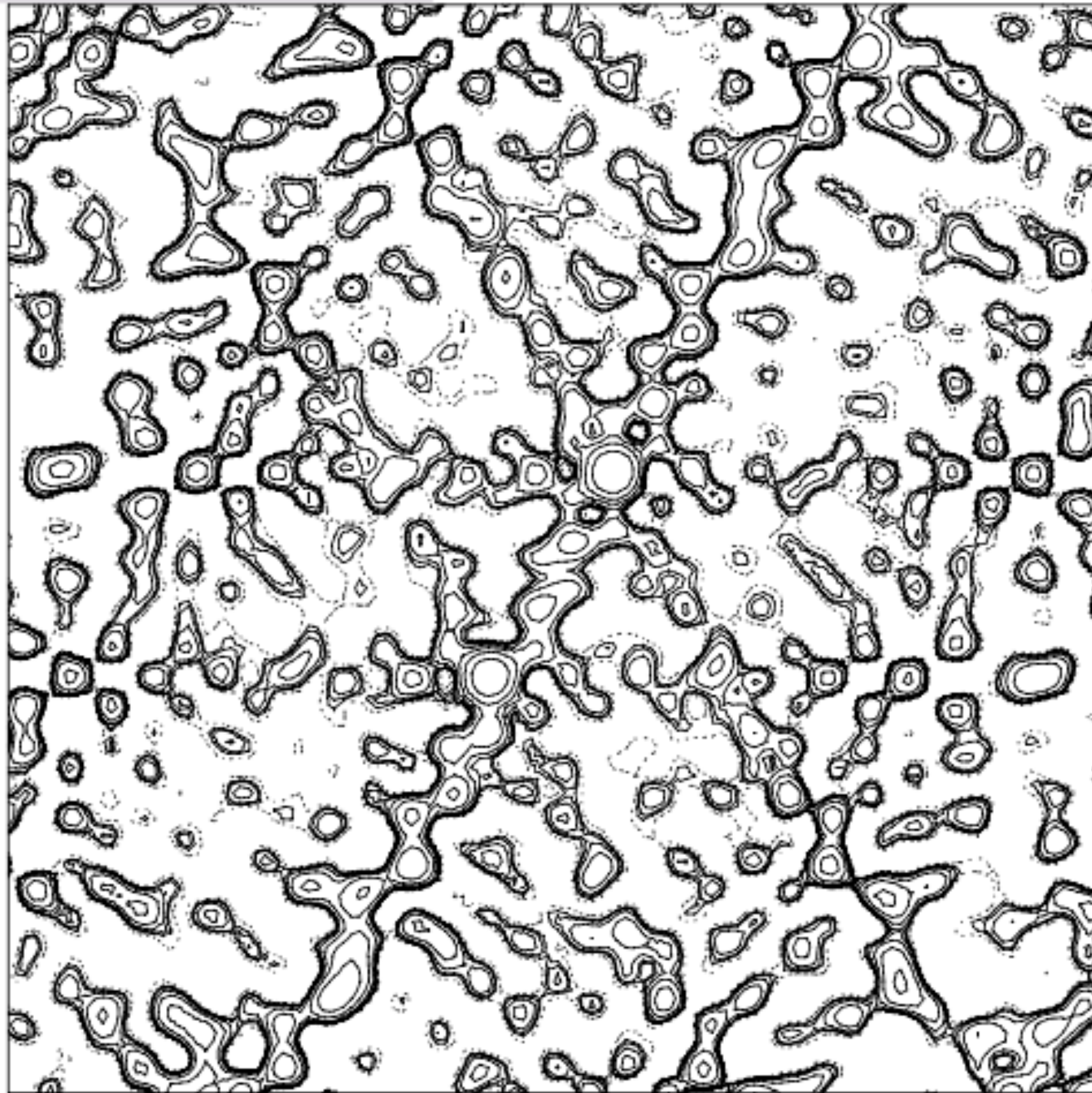


*remove
PSF*



CLEAN fundamentals

Jackson 2008



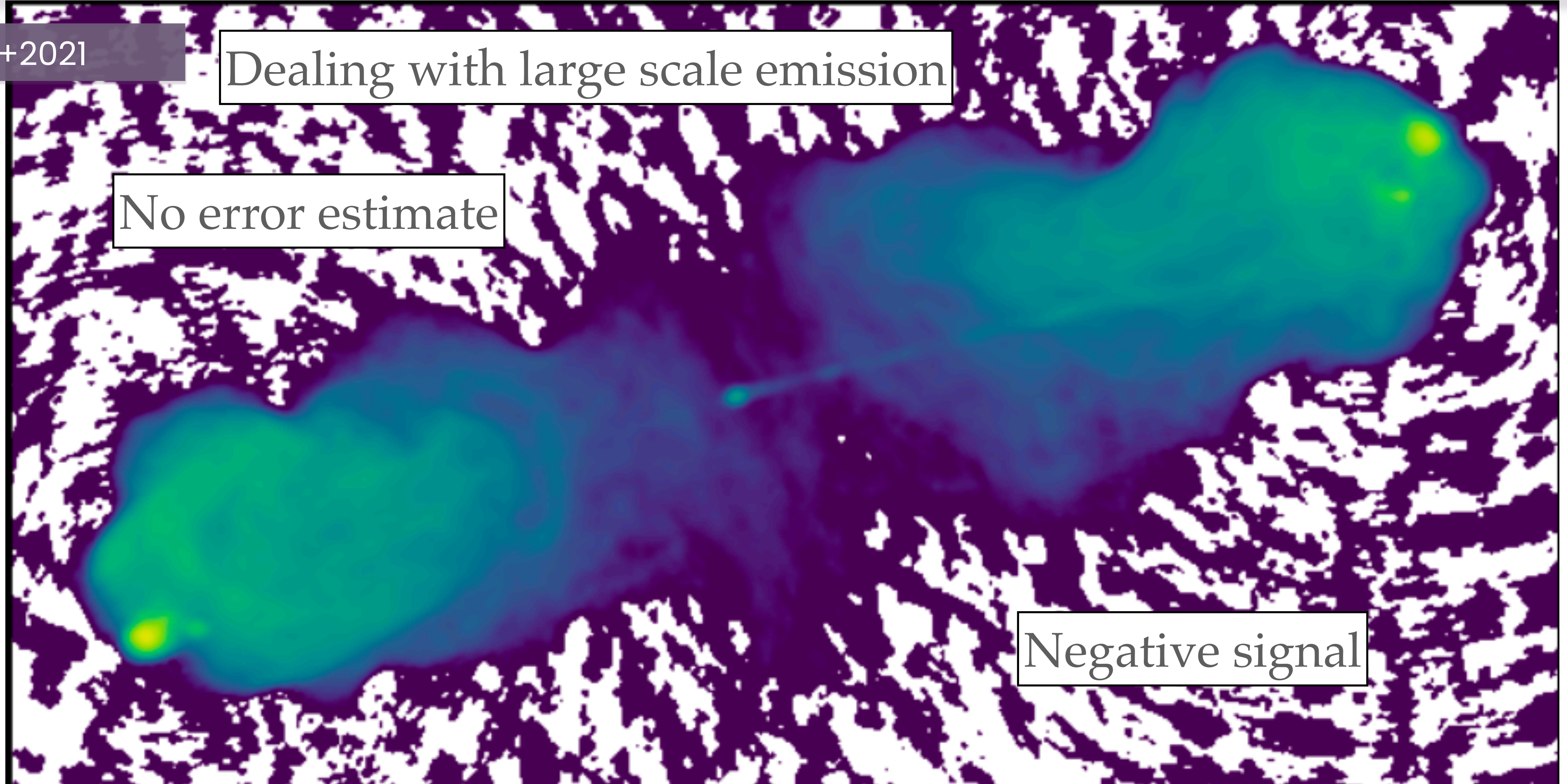
Limitations of CLEAN

Arras+2021

Dealing with large scale emission

No error estimate

Negative signal



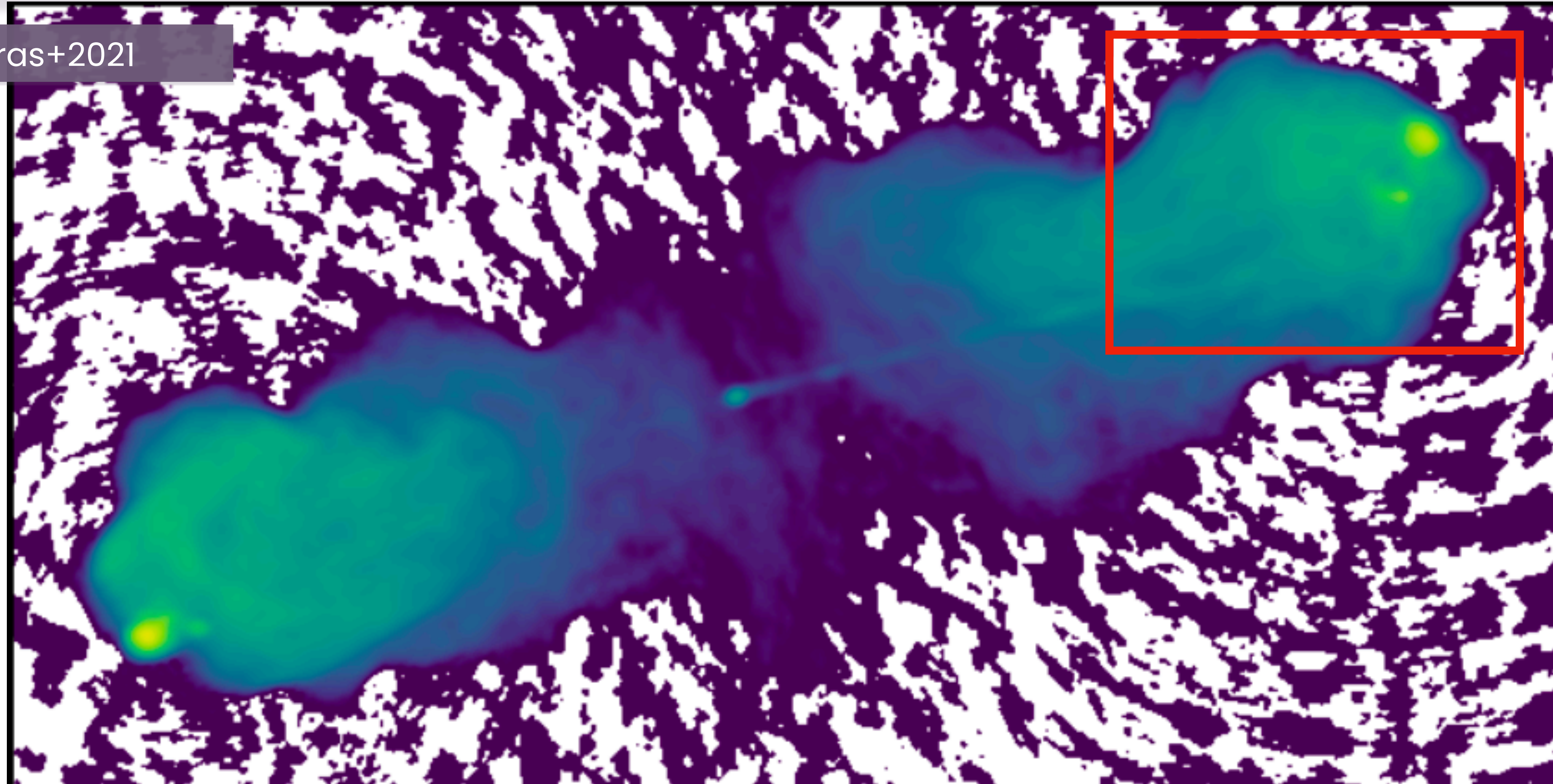
$$\mathcal{P}(s|d) = \frac{\mathcal{P}(d|s)\mathcal{P}(s)}{\mathcal{P}(d)}$$

RESOLVE algorithm

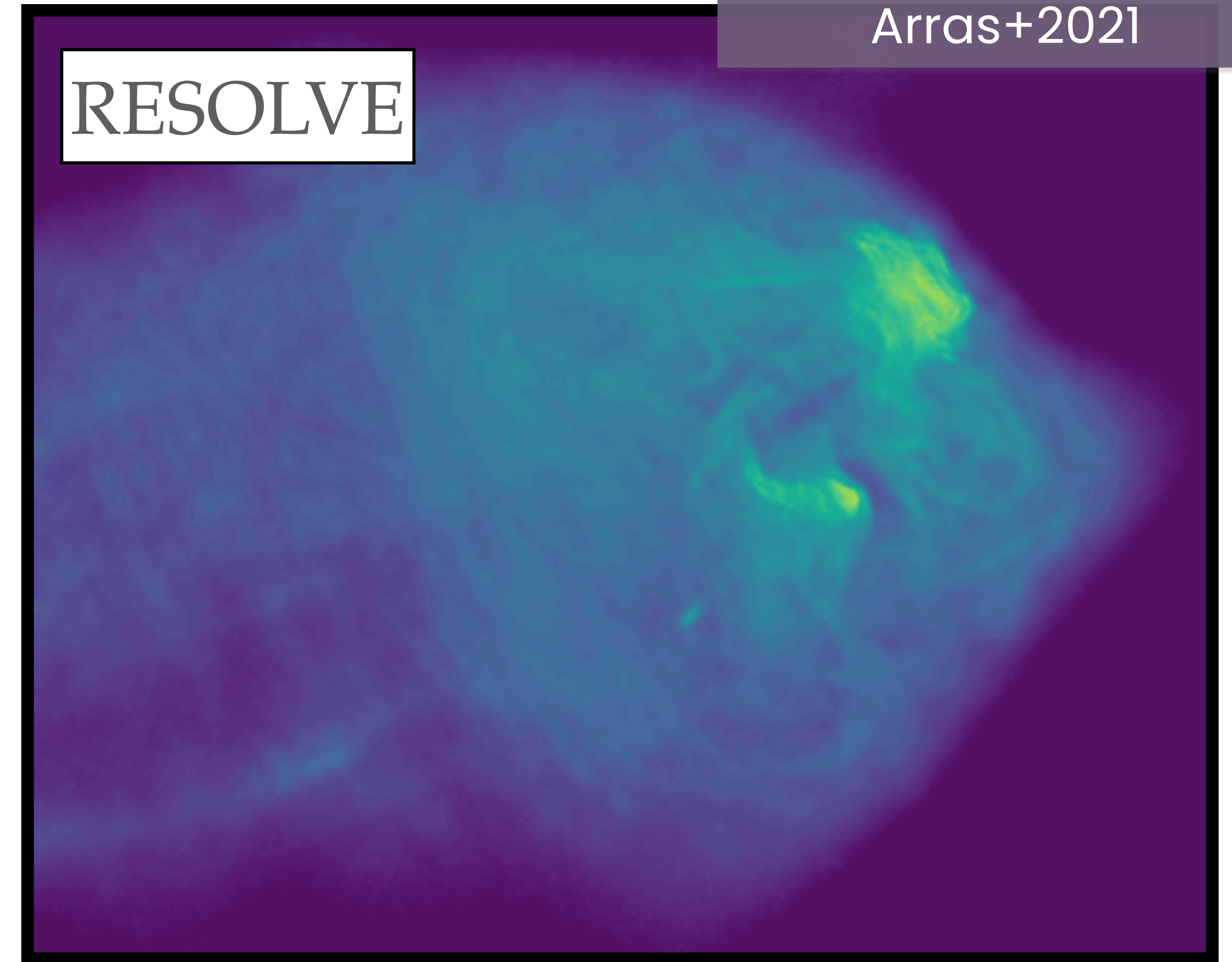
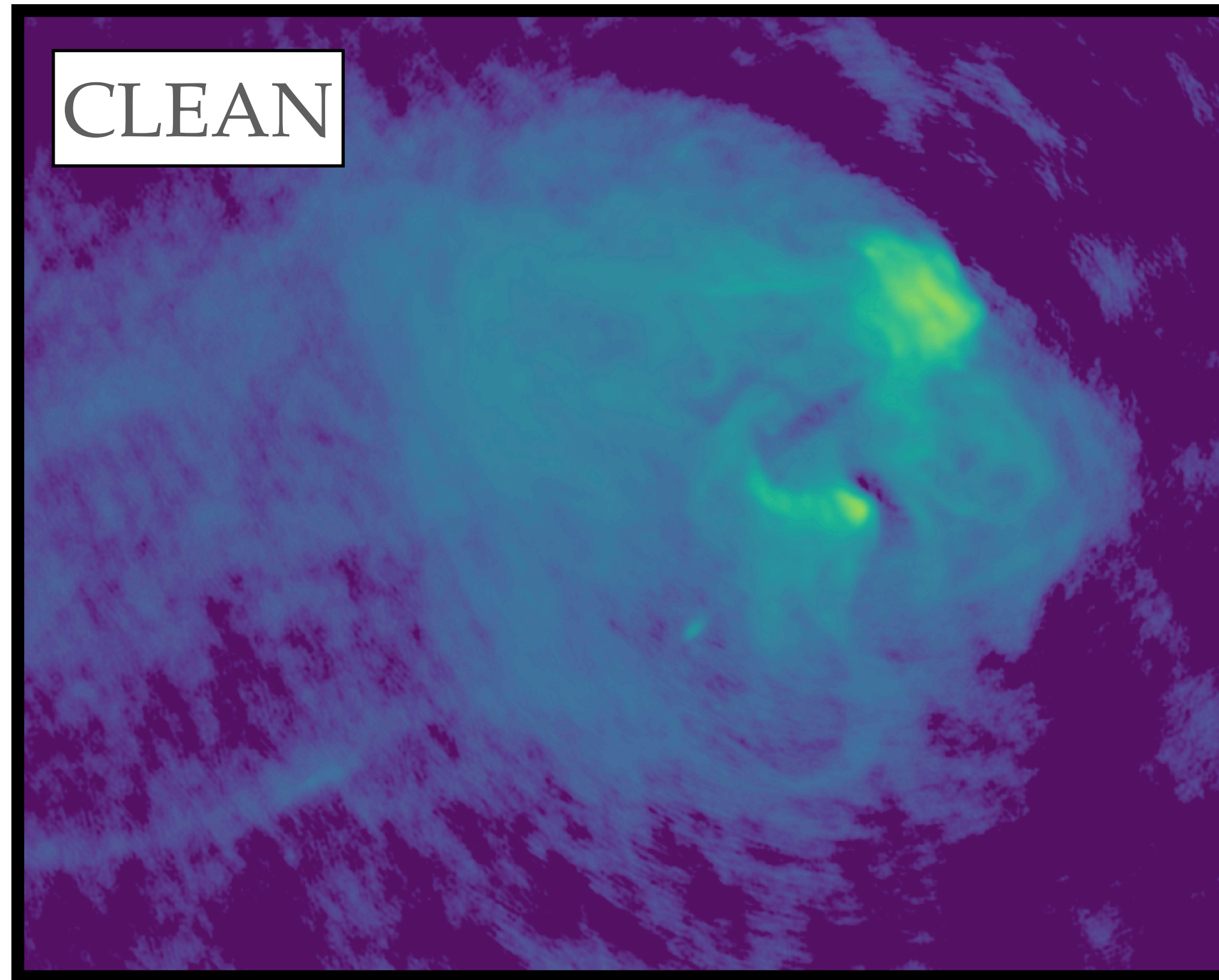
Enßlin+2009, Junklewitz+2014, Arras+2018

Comparison of RESOLVE and CLEAN algorithms – VLA test

Arras+2021

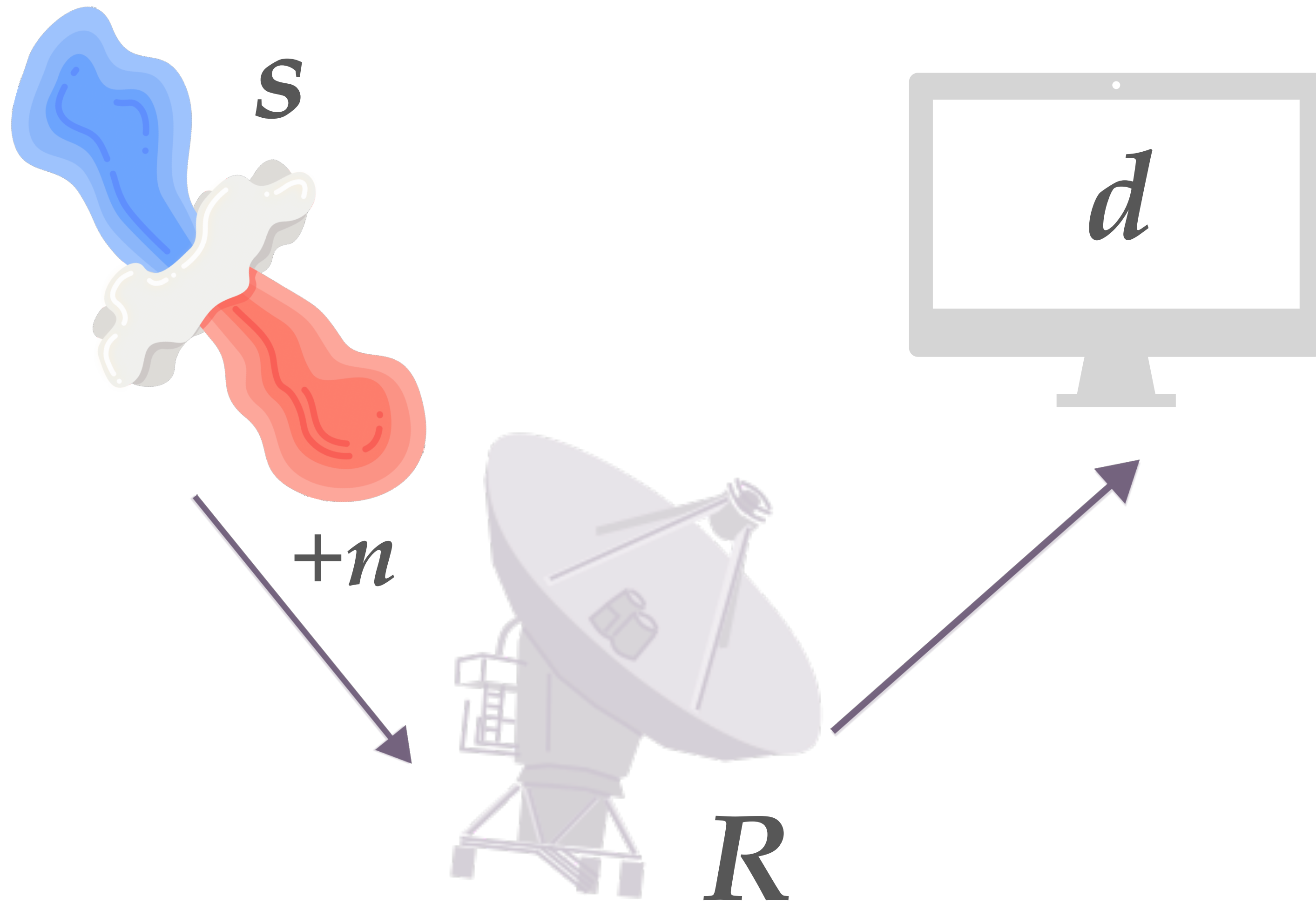


Comparison of RESOLVE and CLEAN algorithms – VLA test



RESOLVE excels in retrieving large-scale emission

Astronomical signal inference



$$d = Rs + n$$

$$\mathcal{P}(s|d) = \frac{\mathcal{P}(d|s)\mathcal{P}(s)}{\mathcal{P}(d)}$$

Information Field Theory (IFT)

Enßlin+2009

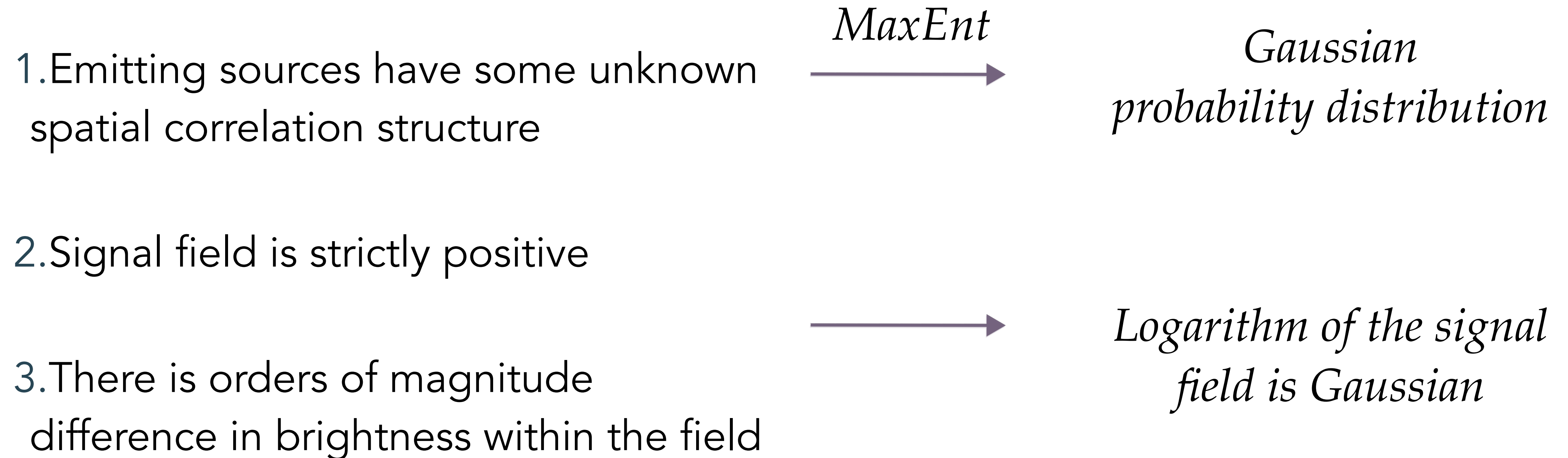
- Enables to use Bayesian inference in the context of field theory
- Treats field as a continuous object (no pixelisation)
- Allows for field theory formalism
- Well fitted to the context of inference of sky brightness from interferometric observation
- Practically: NIFTy python package (Reinecke+2018, Selig+2013, Arras+2019)

Minimum information on the field

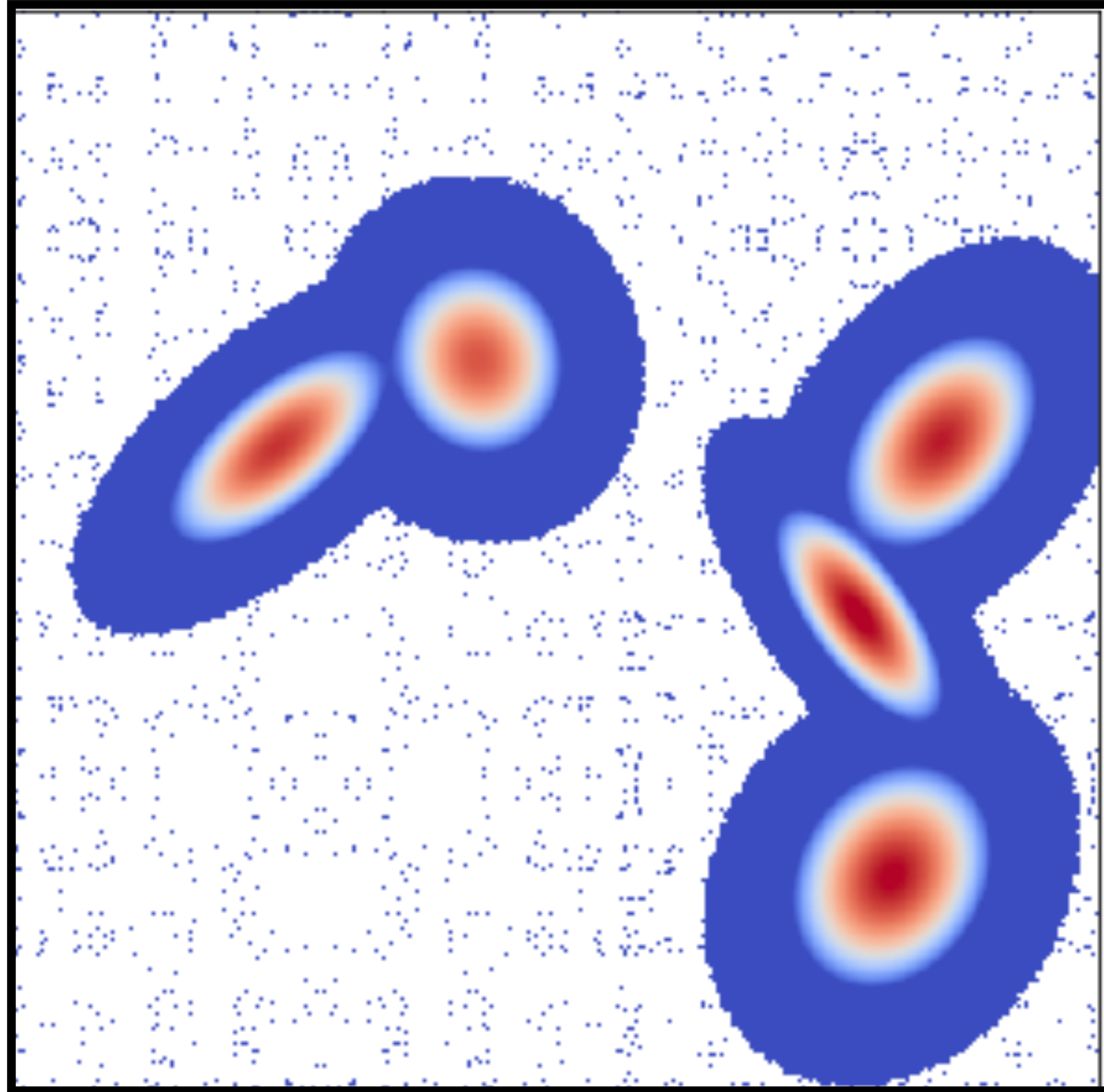
1. Emitting sources have some unknown spatial correlation structure
2. Signal field is strictly positive
3. There is orders of magnitude difference in brightness within the field

Minimum information on the field

Junklewitz+2014



$$d = RI + n = RI_0 e^s + n$$

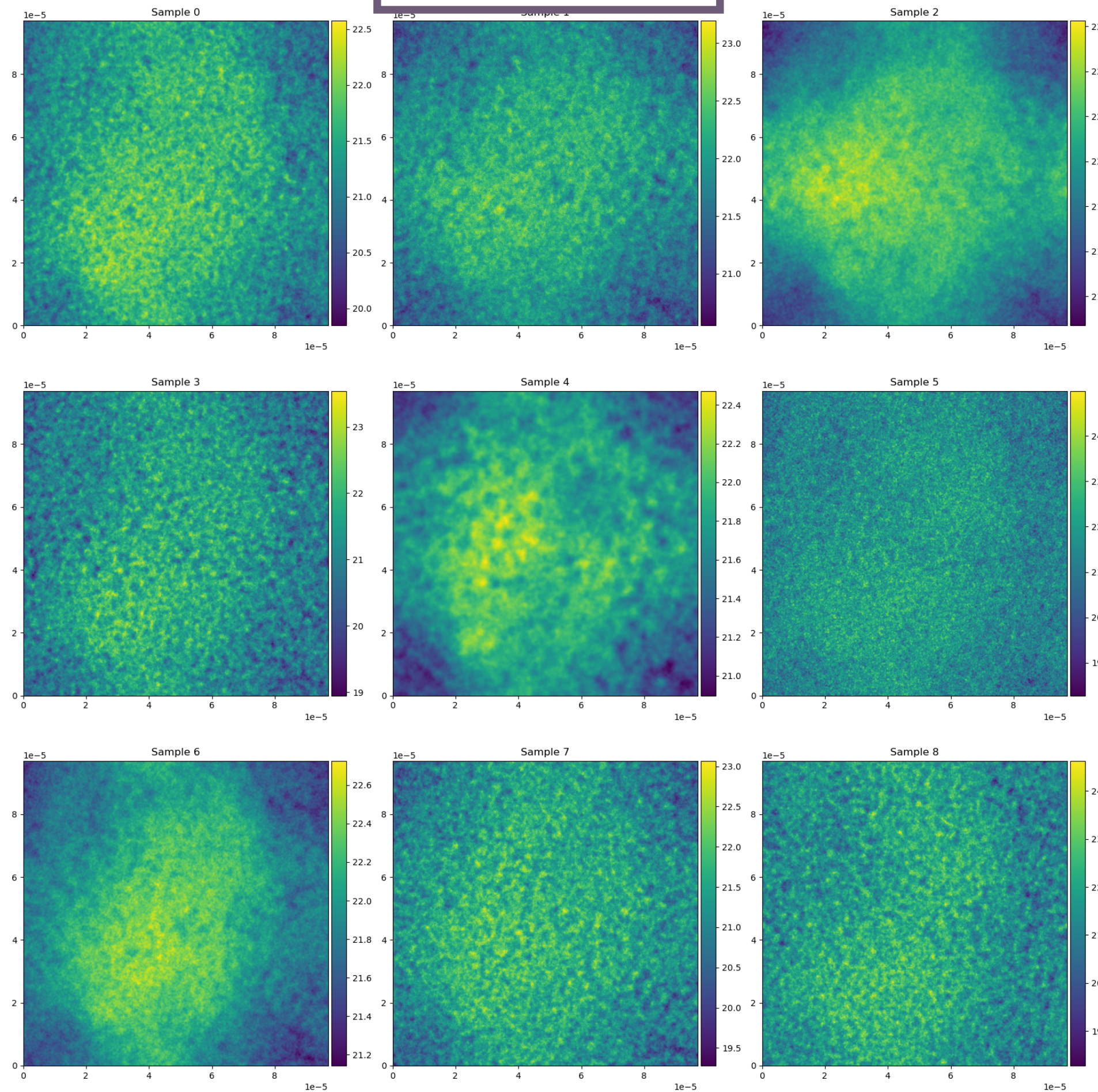


RESOLVE application to simulated dataset

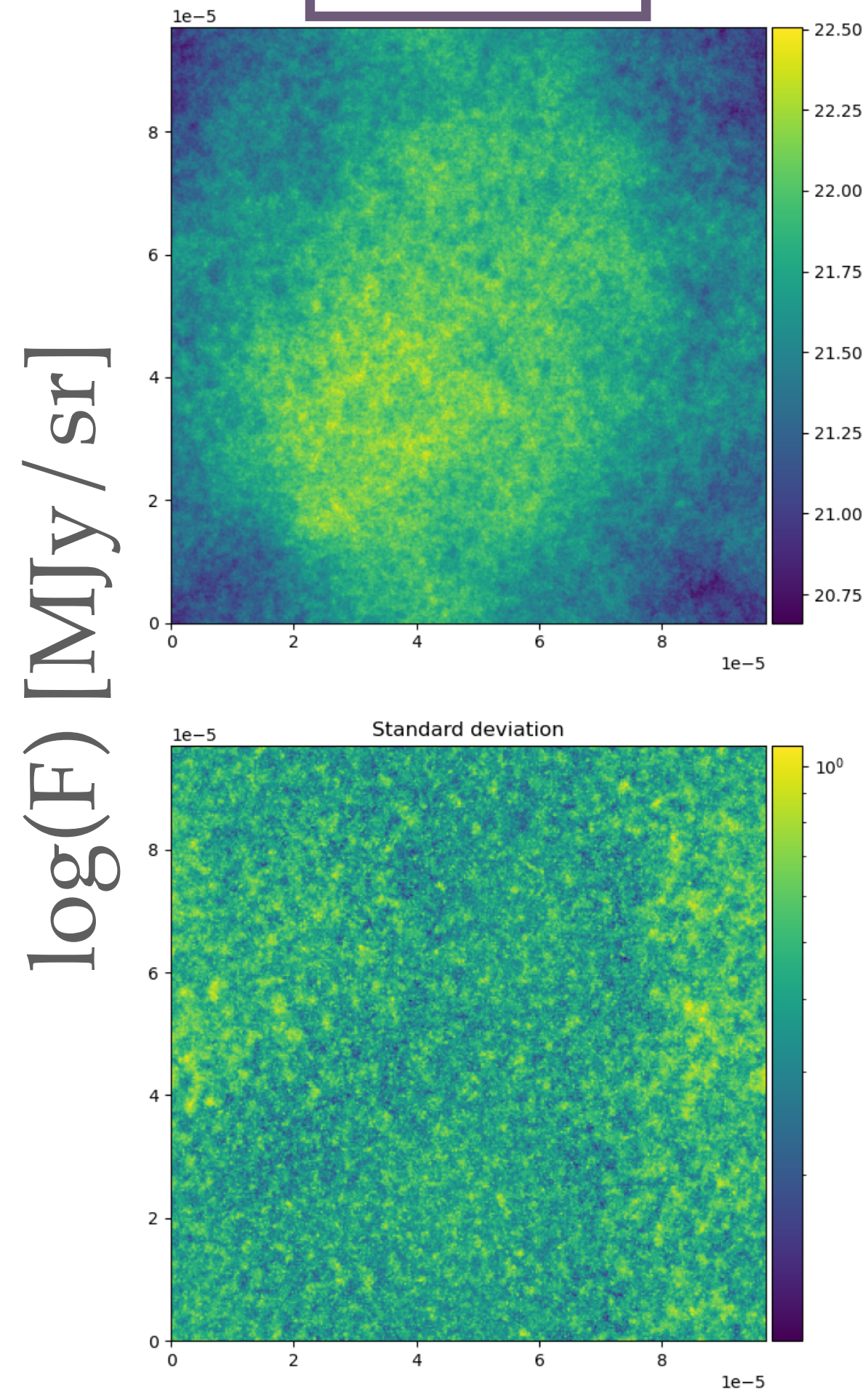
*A simulation of Gaussian
continuum sources*

Iterations of RESOLVE

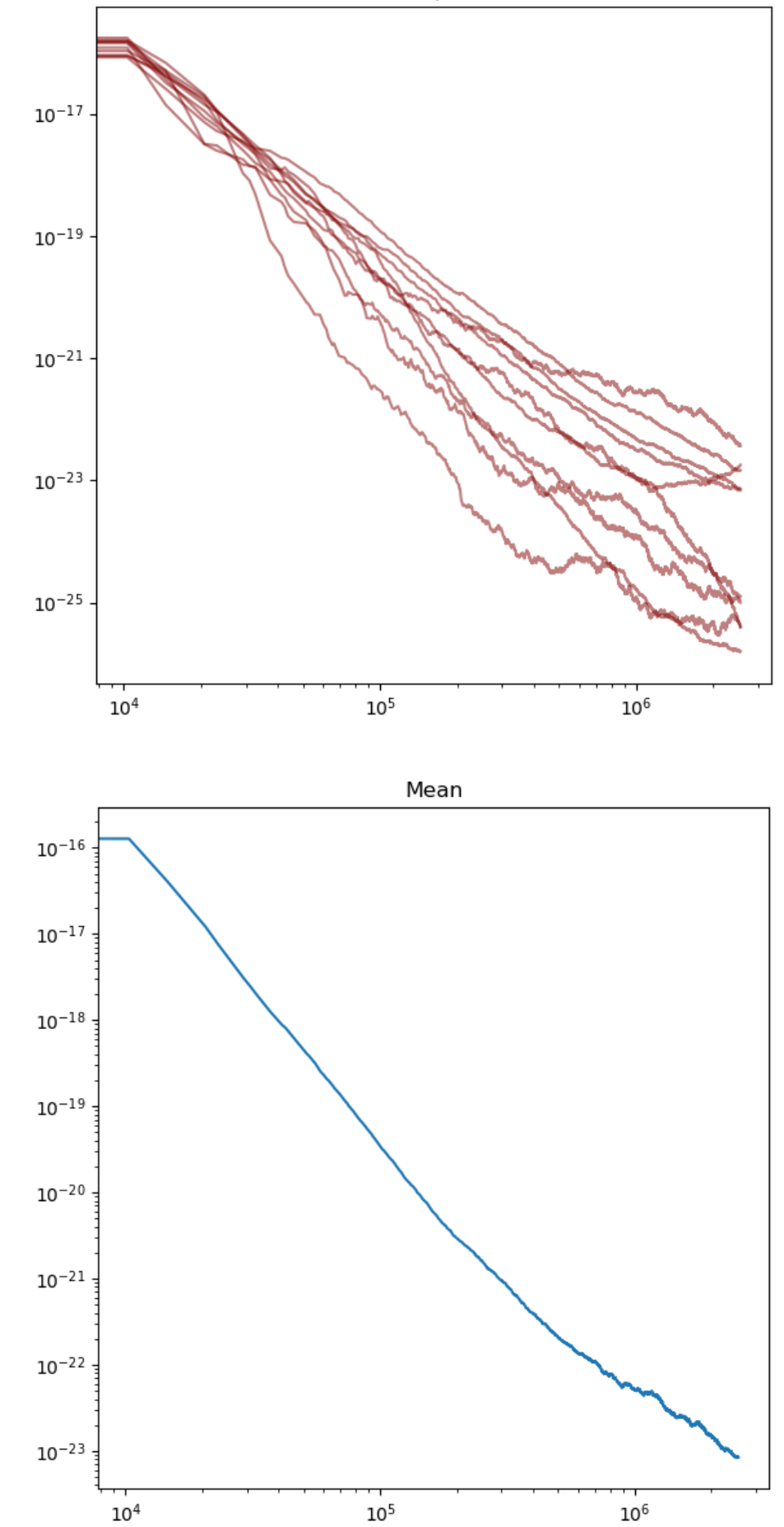
Samples



Means



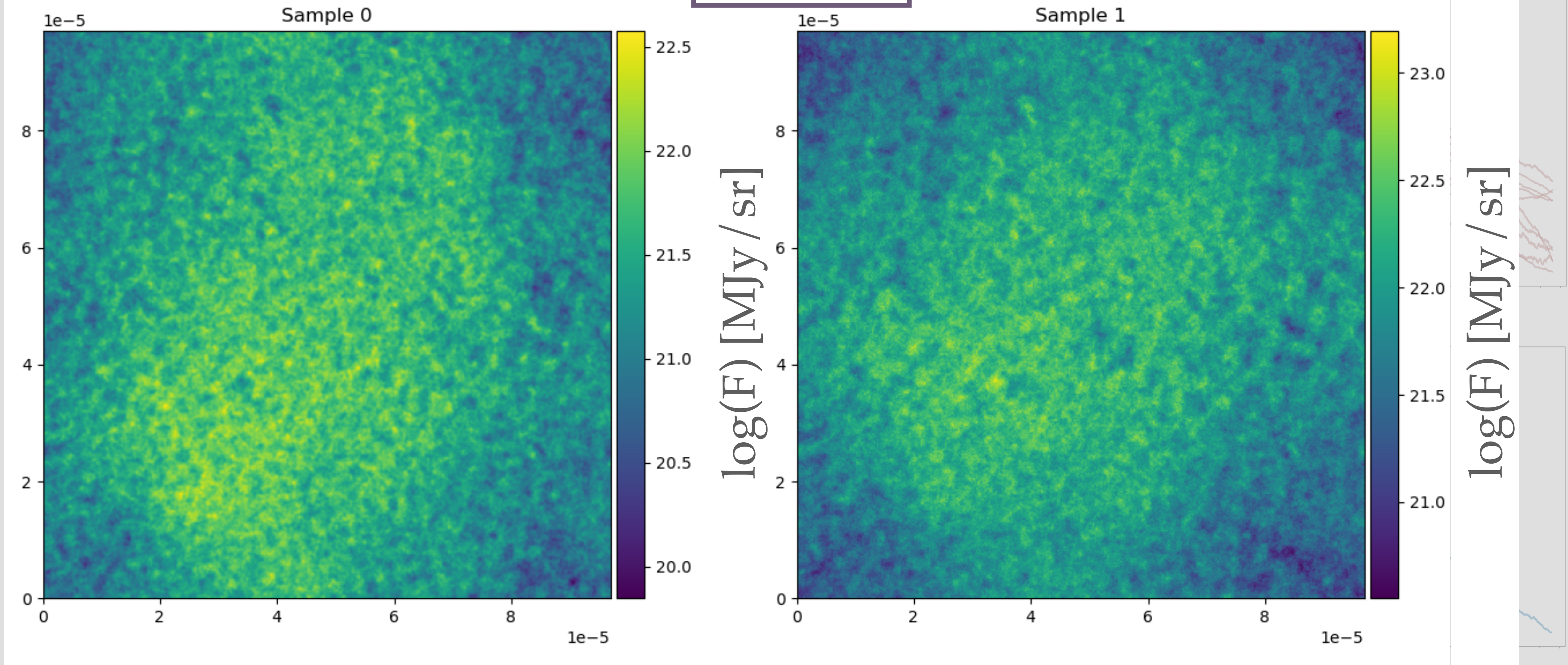
Power spectrum



$\log(F)$ [MJy / sr]

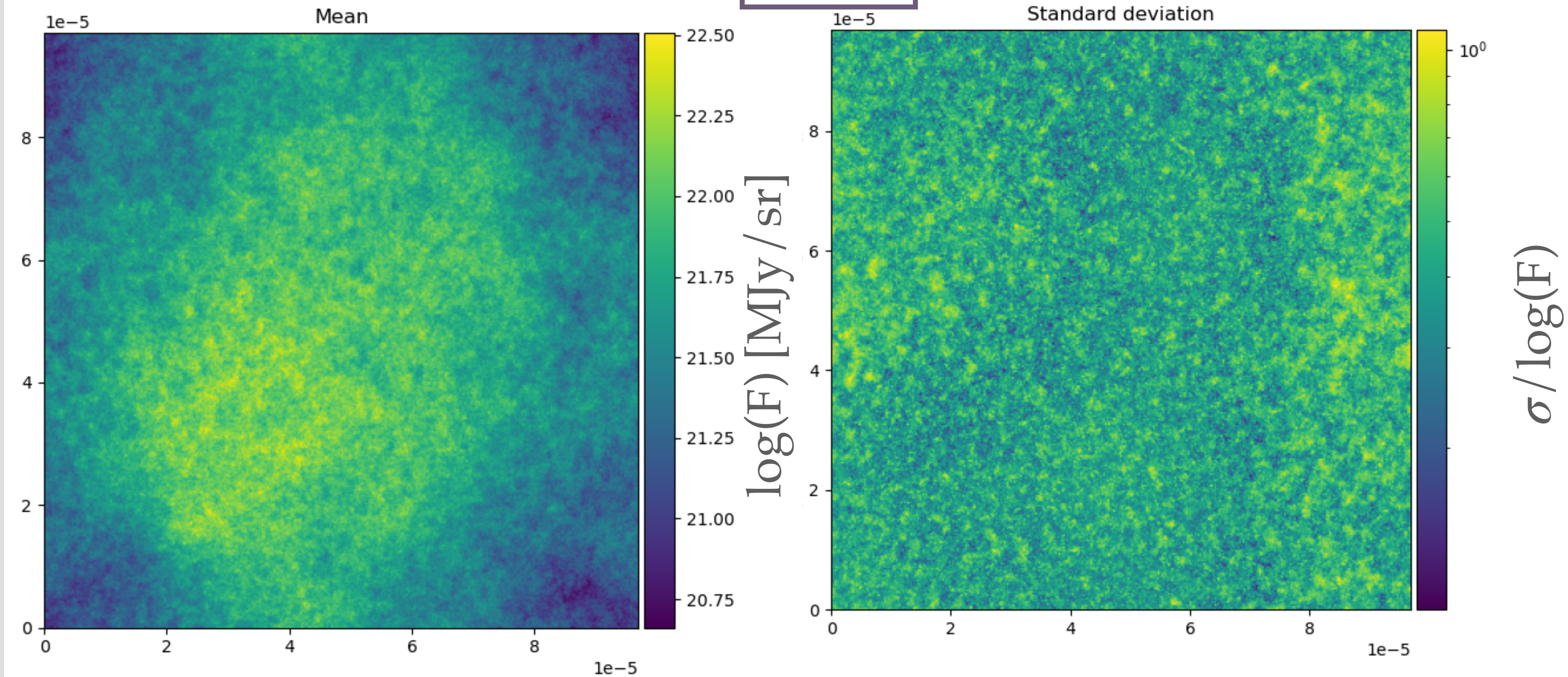
Iterations of RESOLVE

Samples



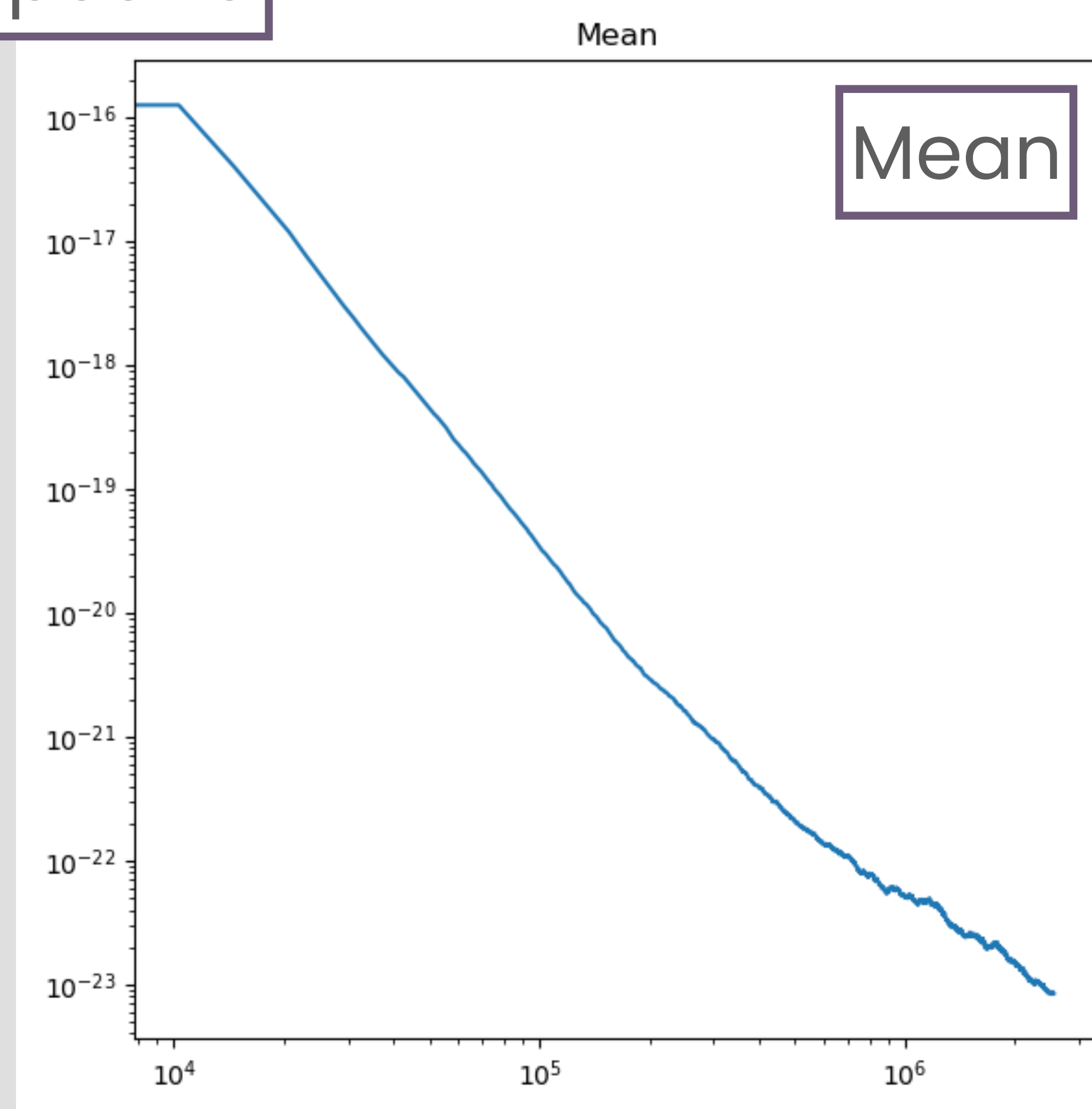
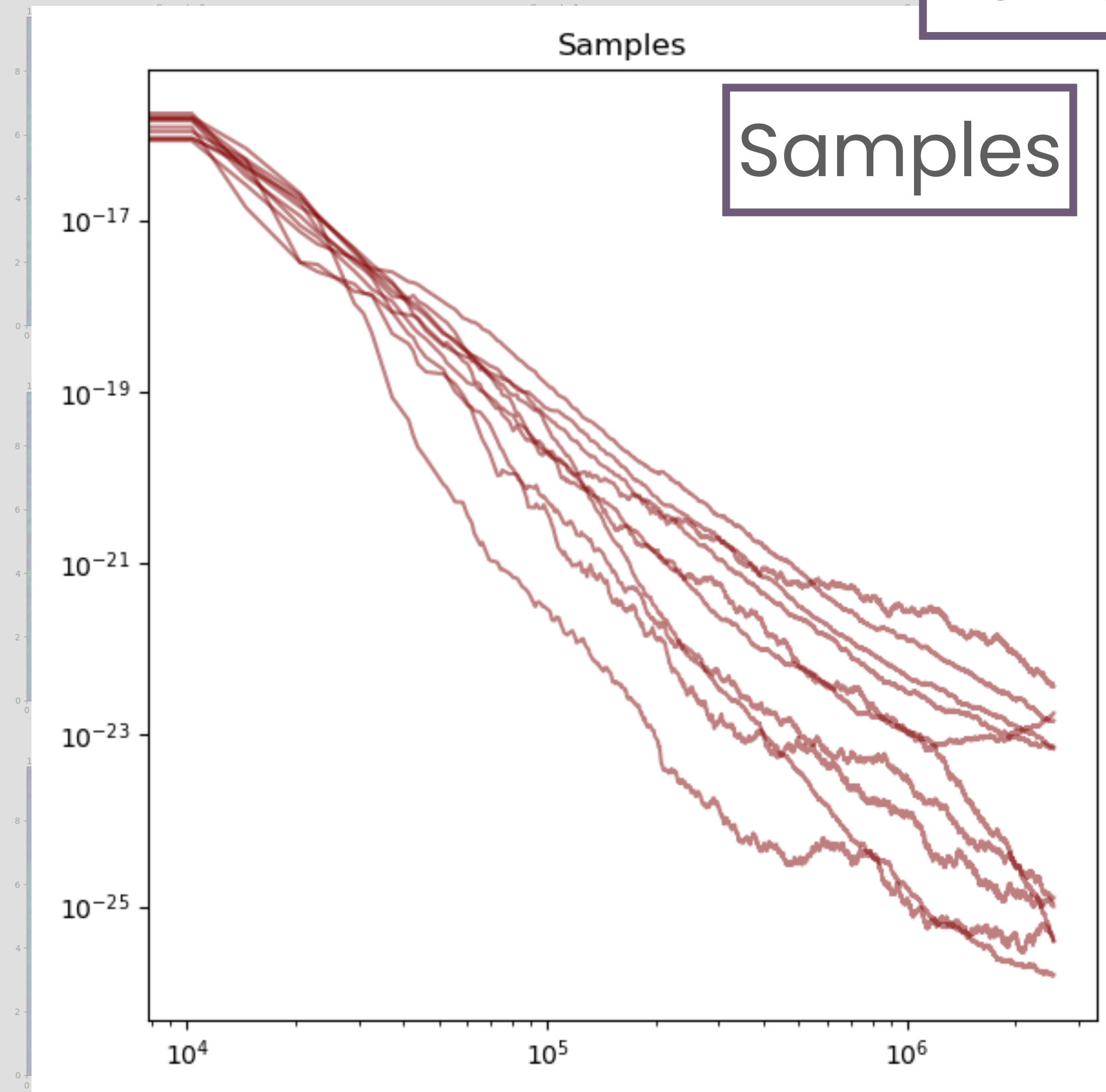
Iterations of RESOLVE

Means



Iterations of RESOLVE

Power spectra



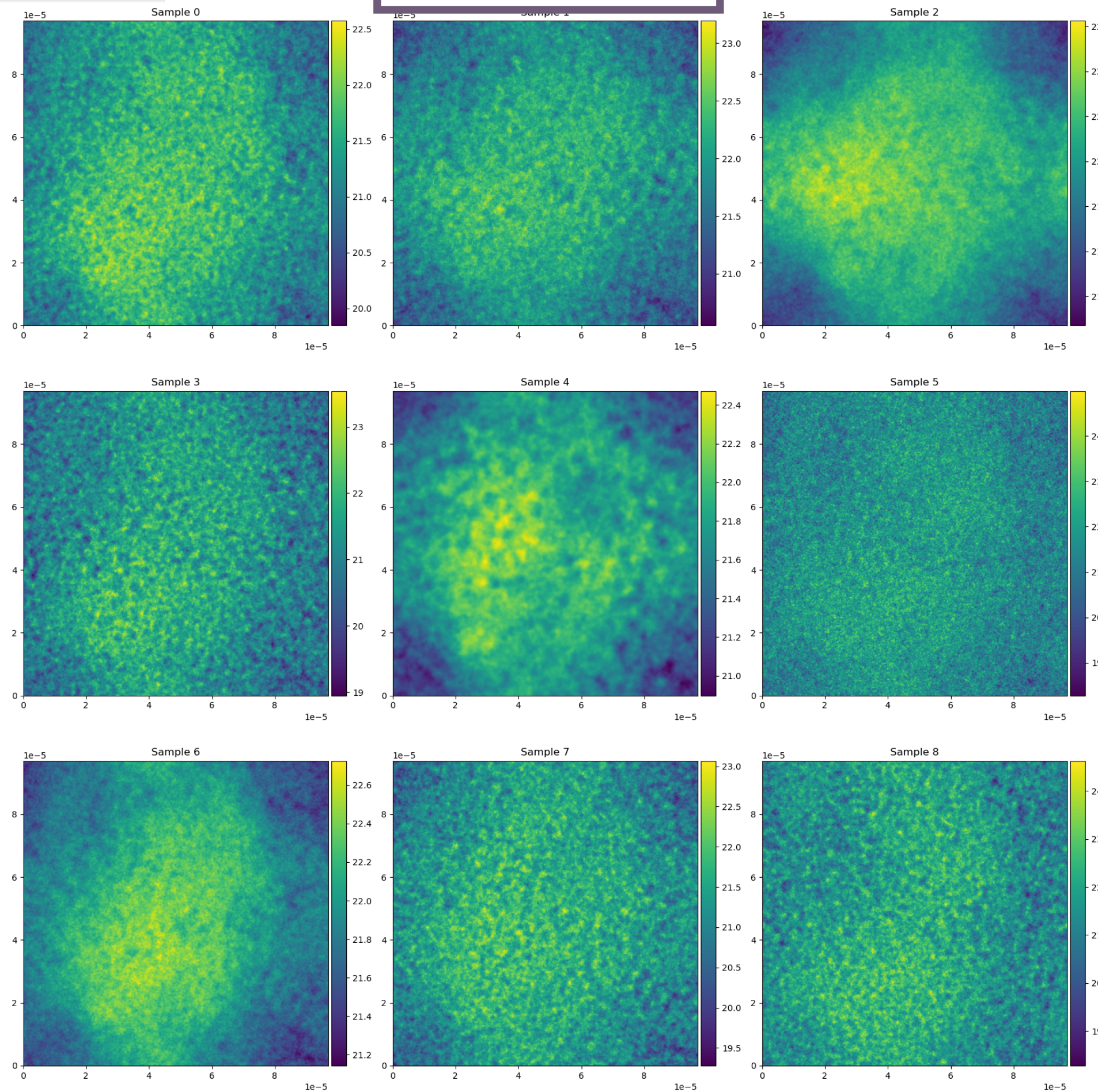
Iterations of RESOLVE

Iter = 0

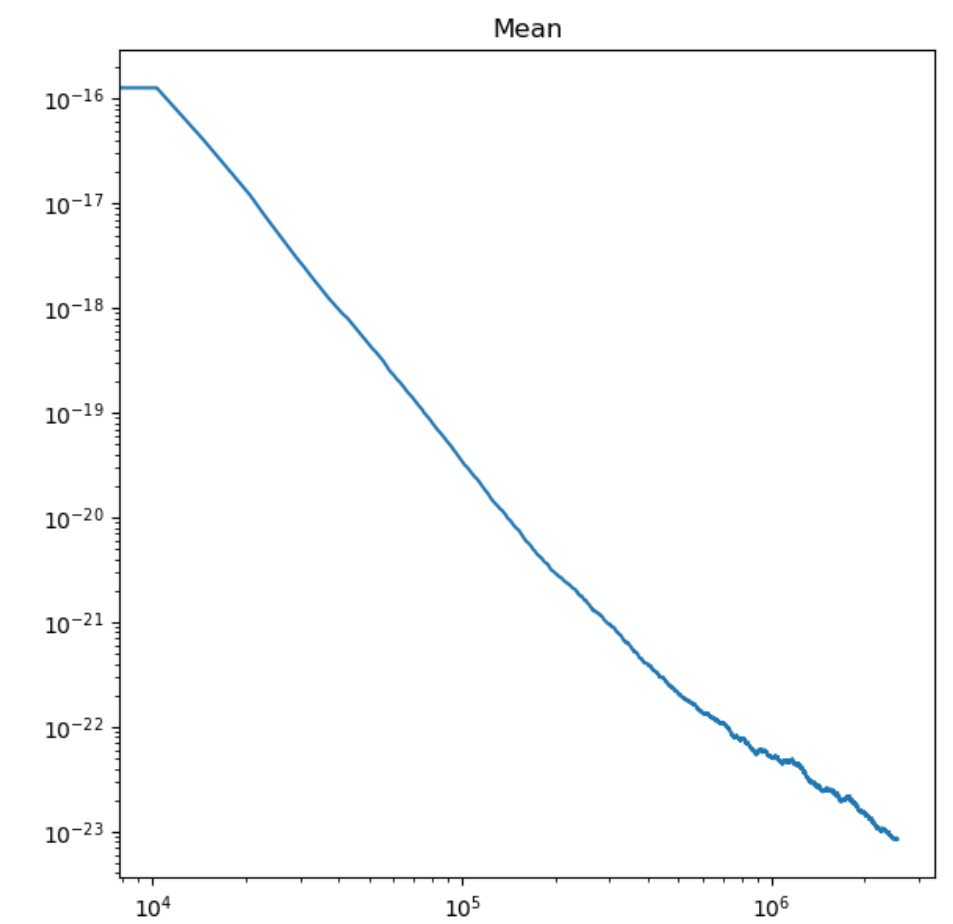
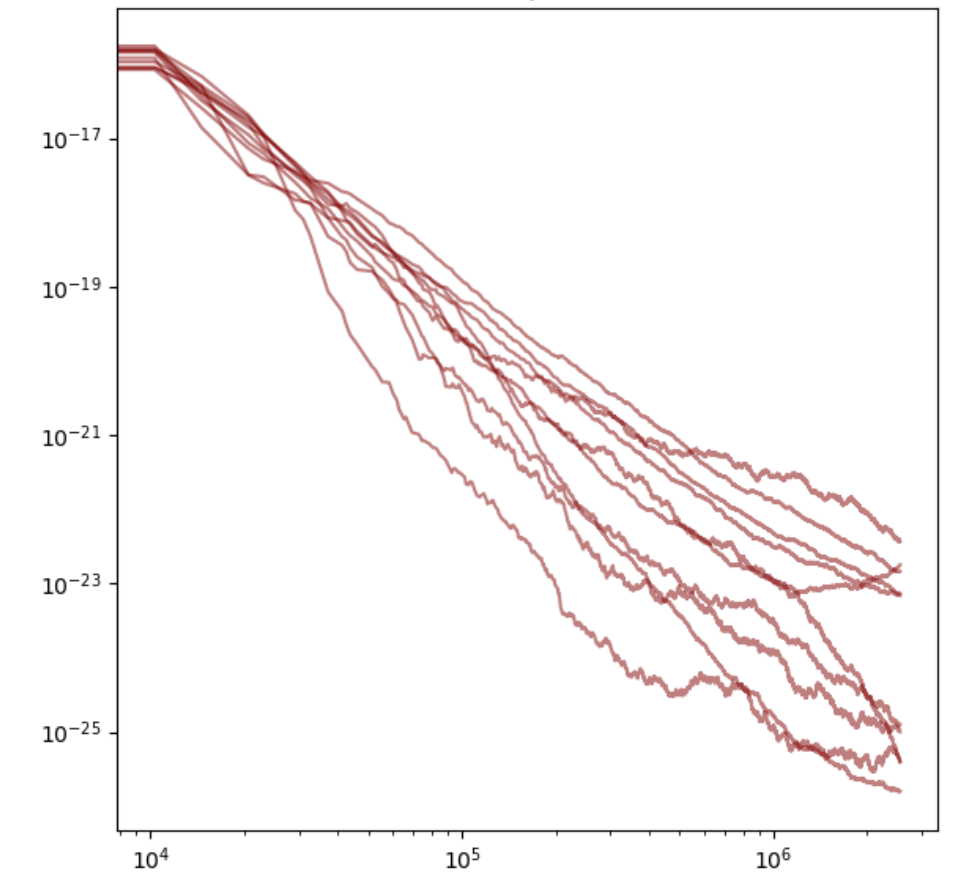
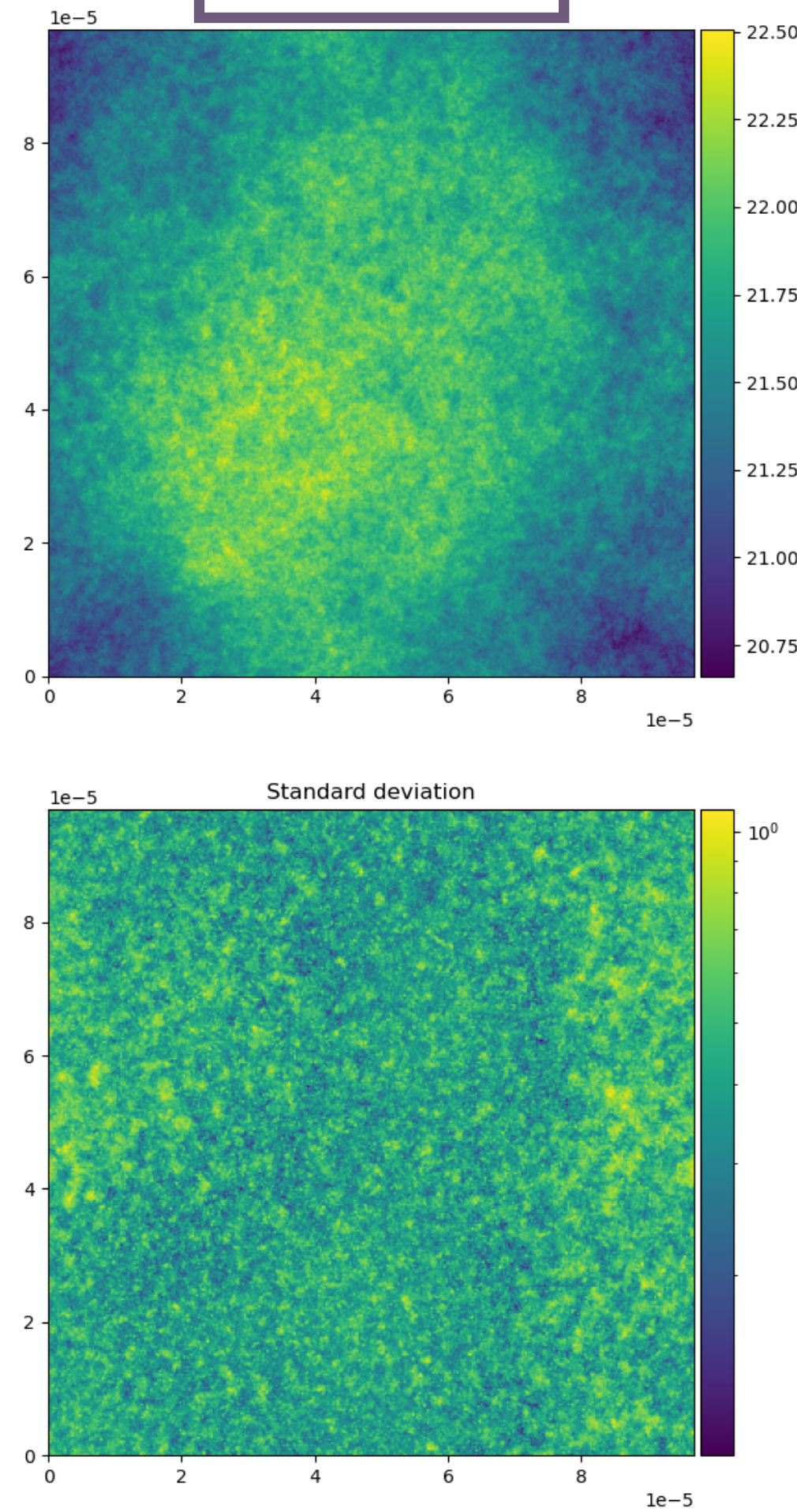
Samples

Means

Power spectrum



$\log(F)$ [MJy / sr]



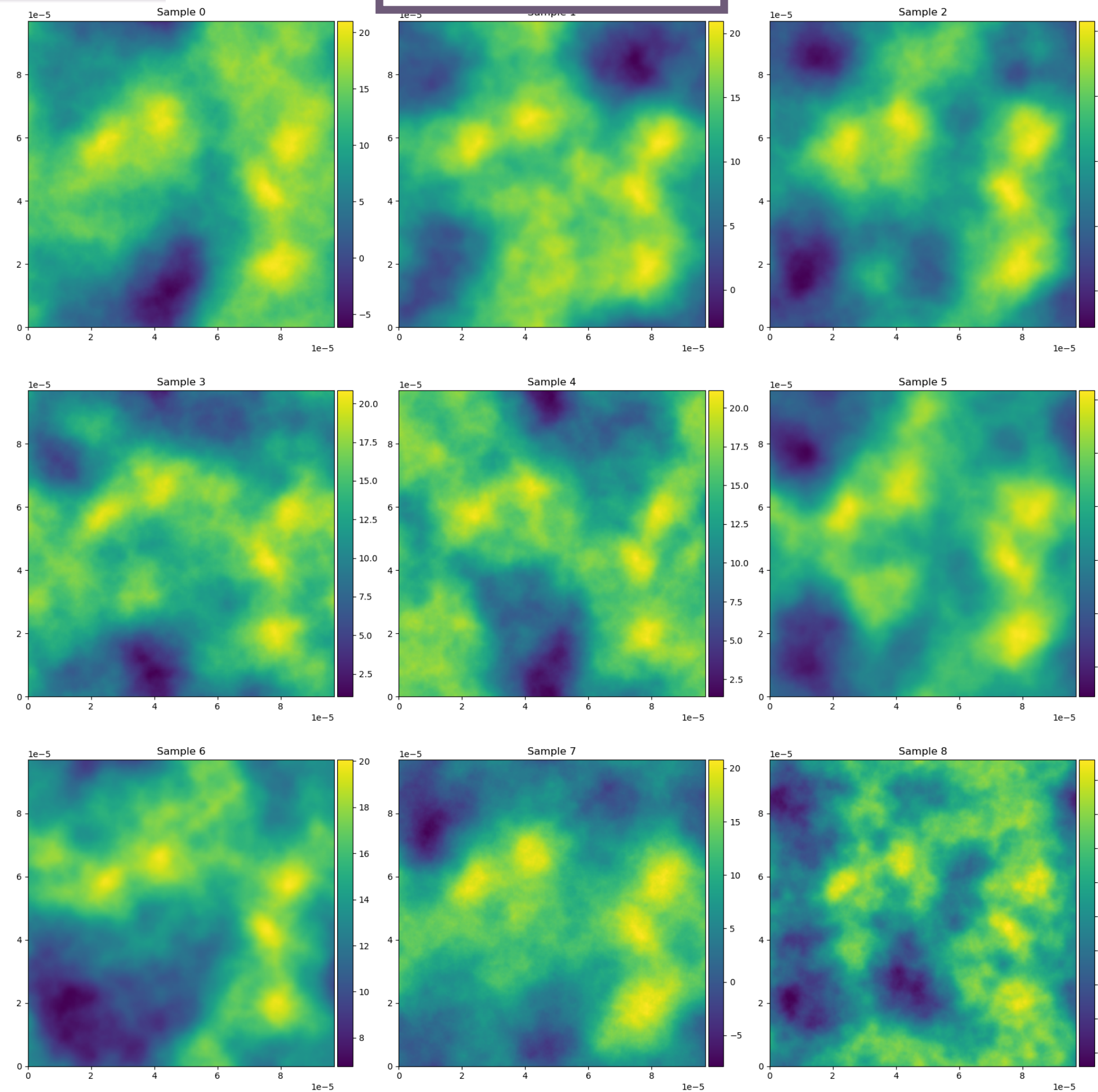
Iterative process

Iter = 5

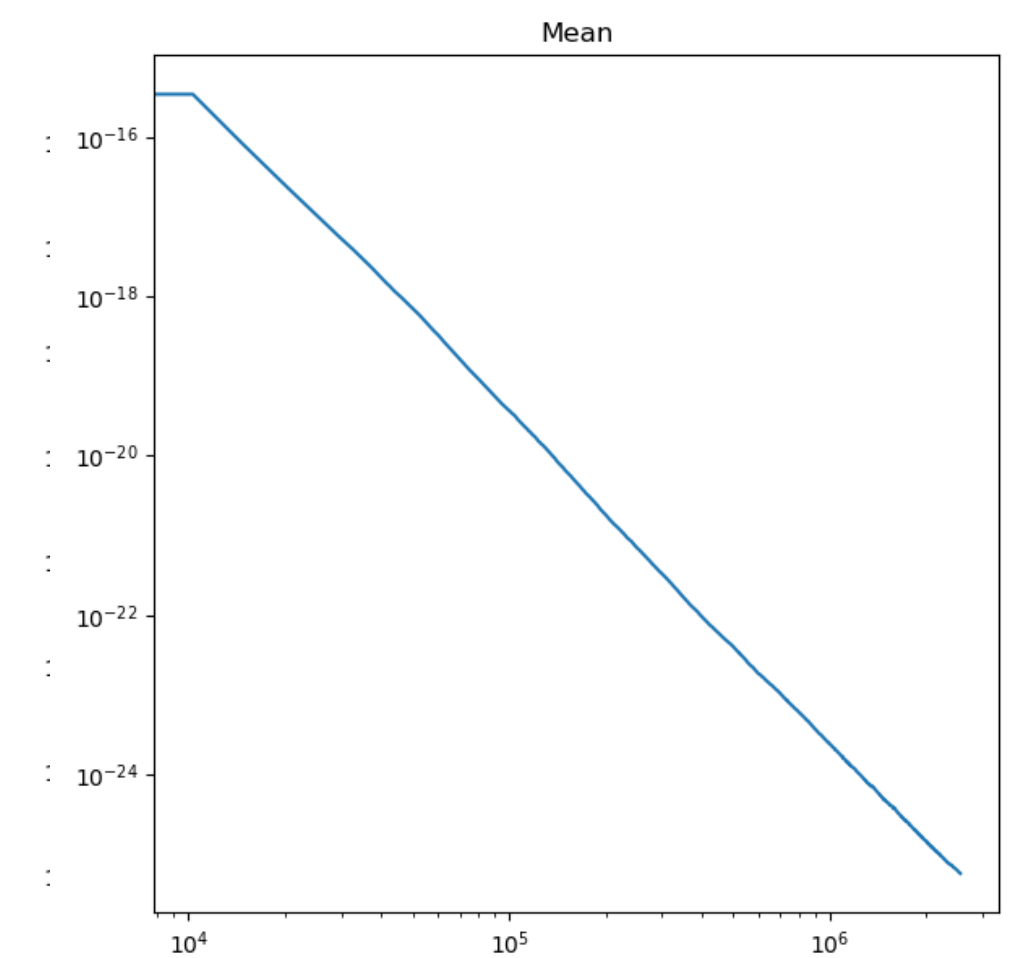
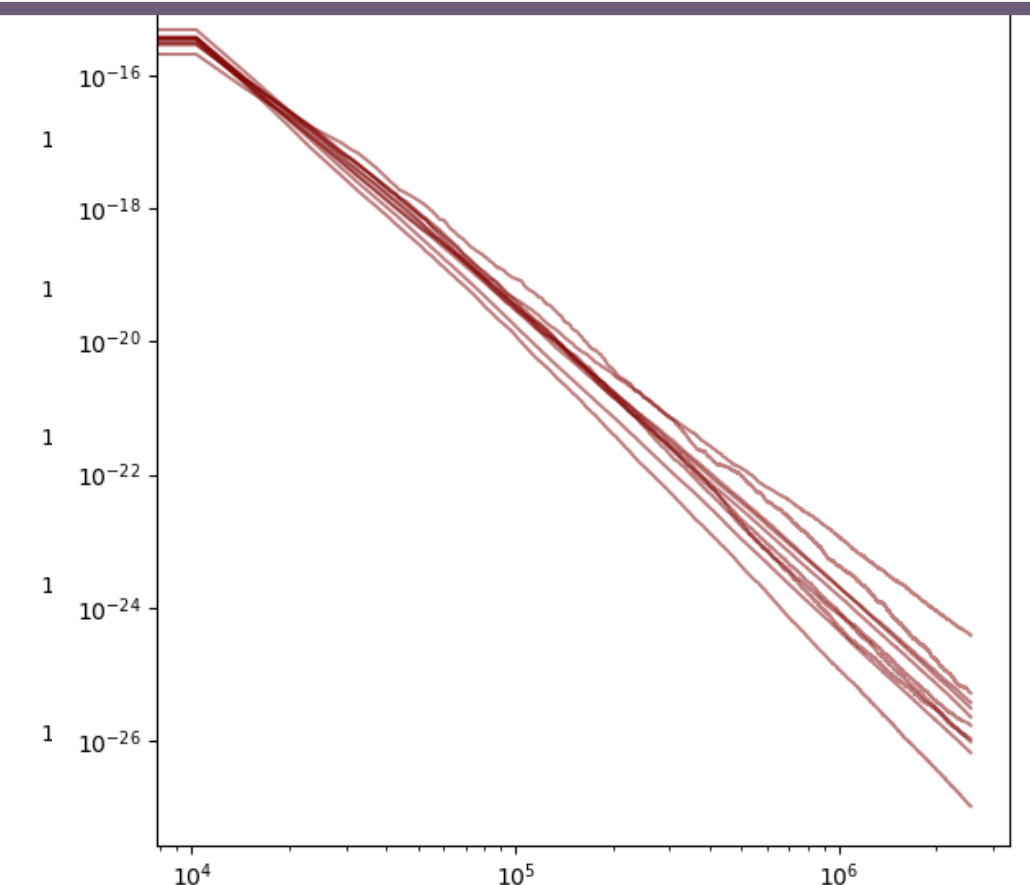
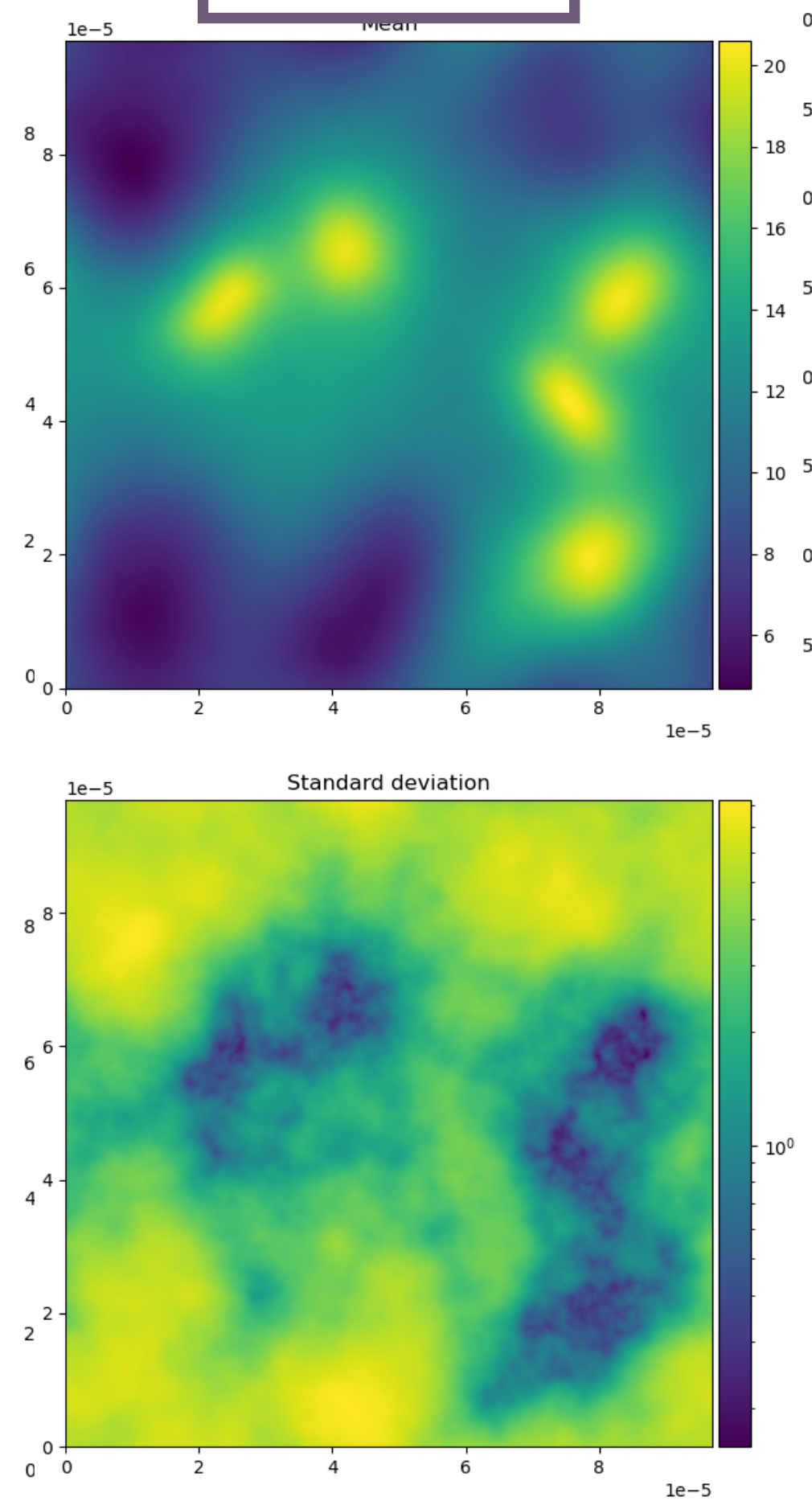
Samples

Means

Power spectrum



$\log(F)$ [MJy / sr]



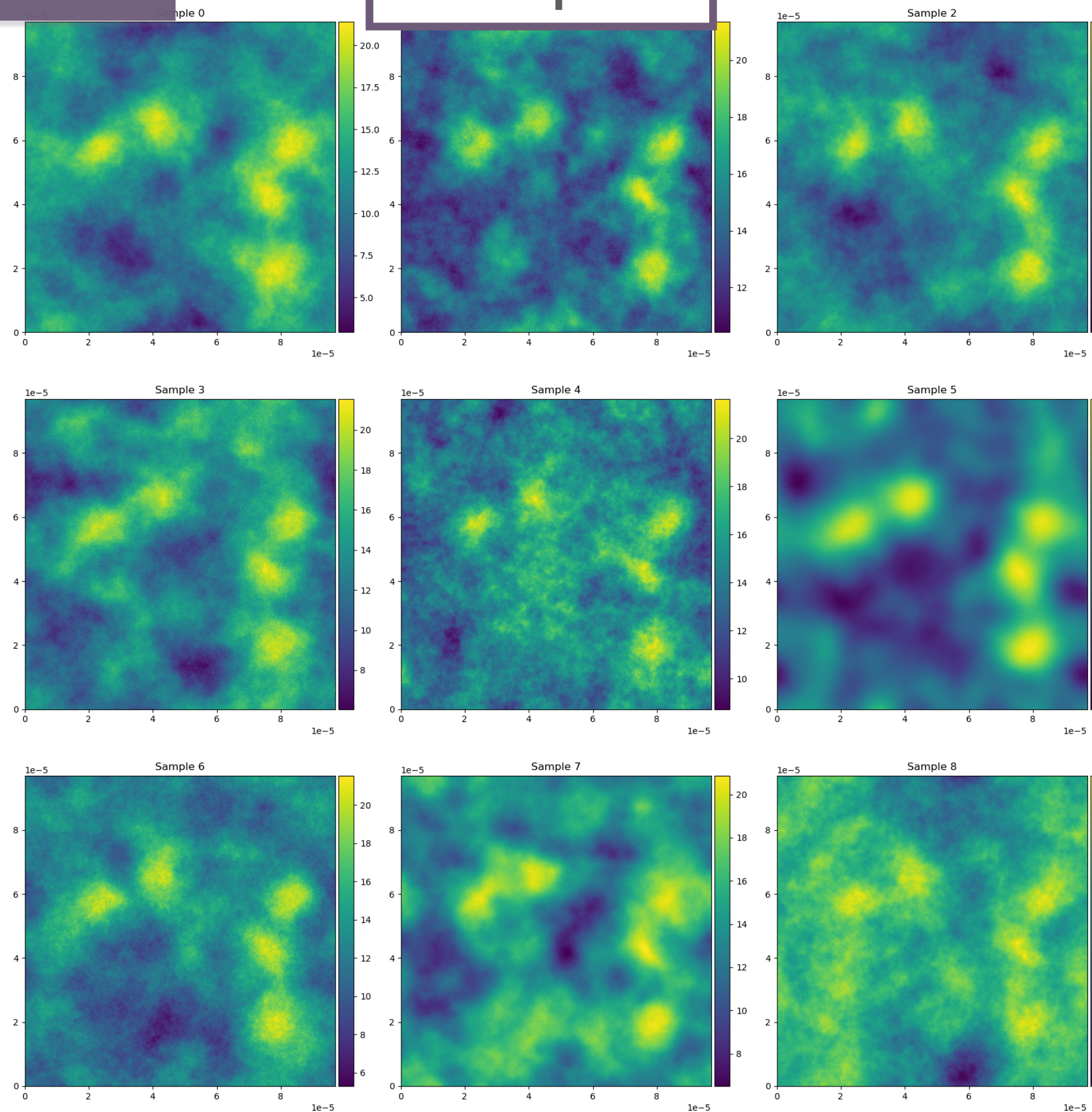
Iterative process

Iter = 23

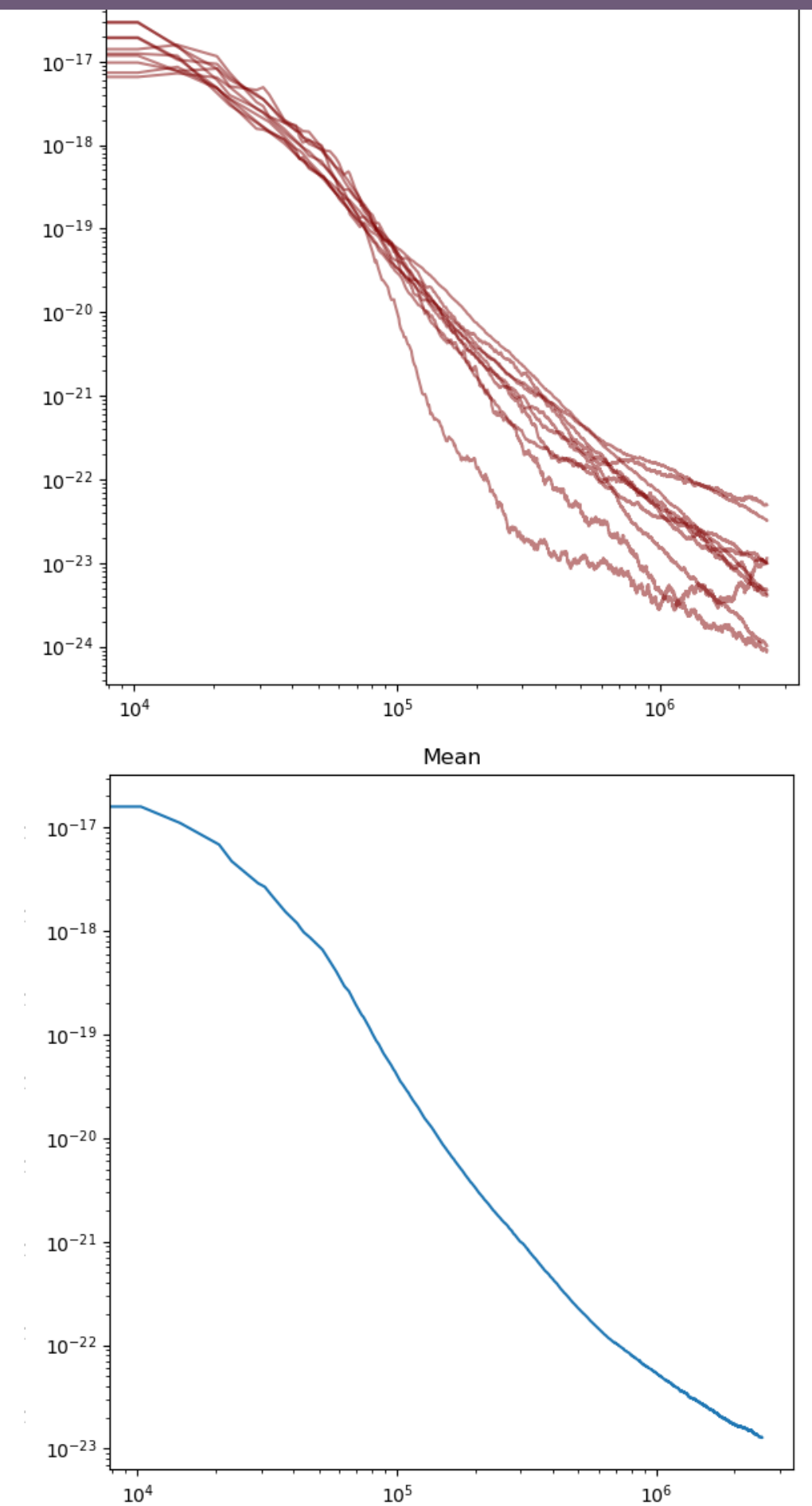
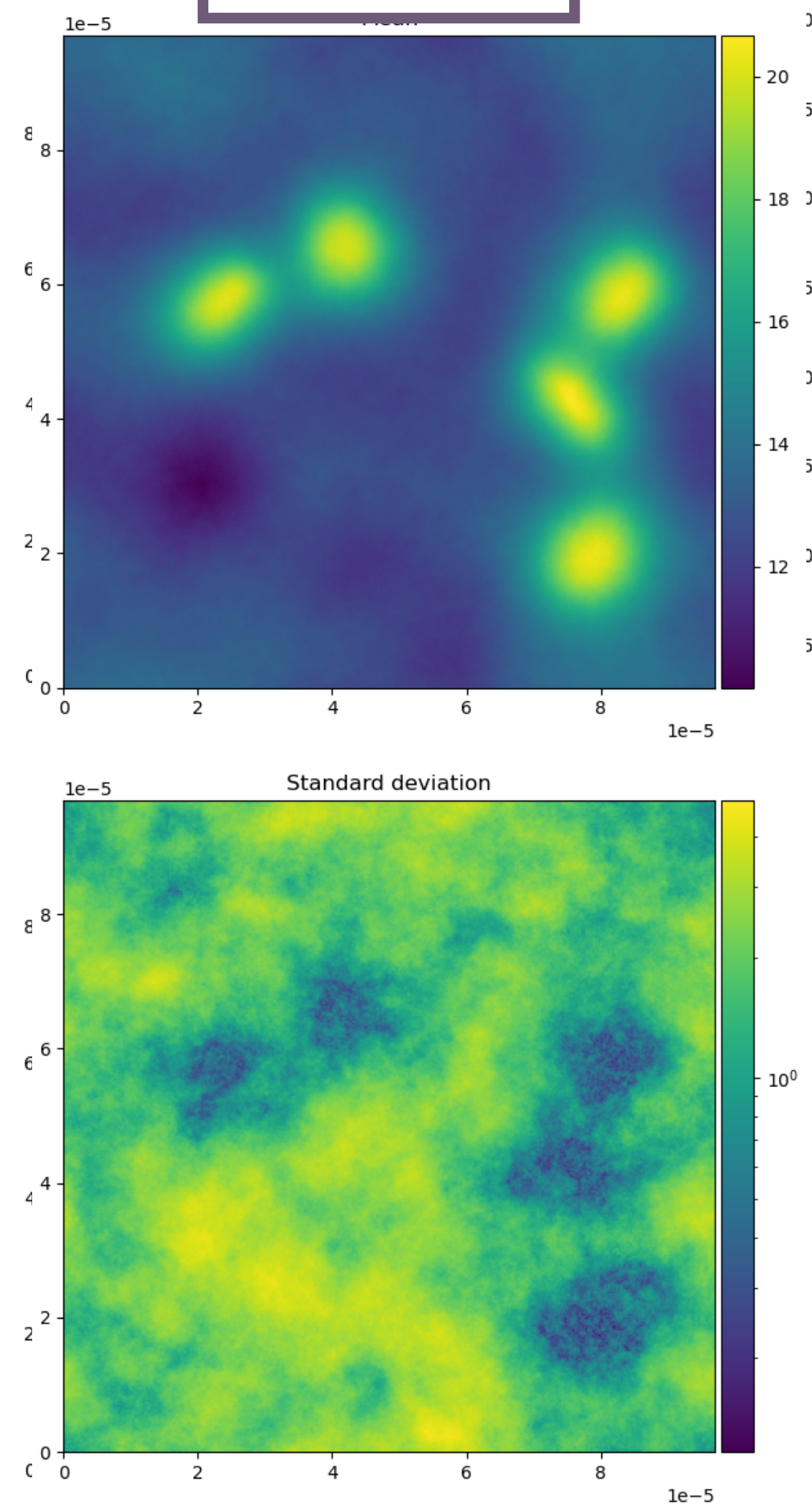
Samples

Means

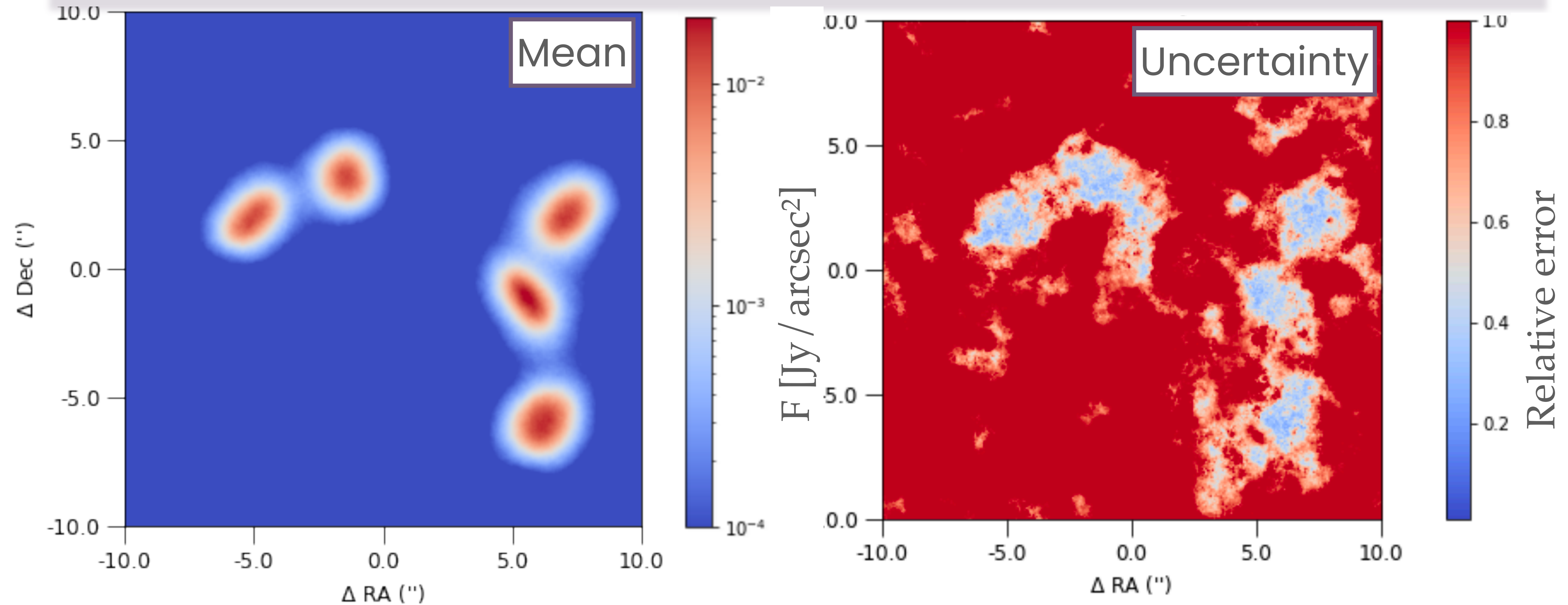
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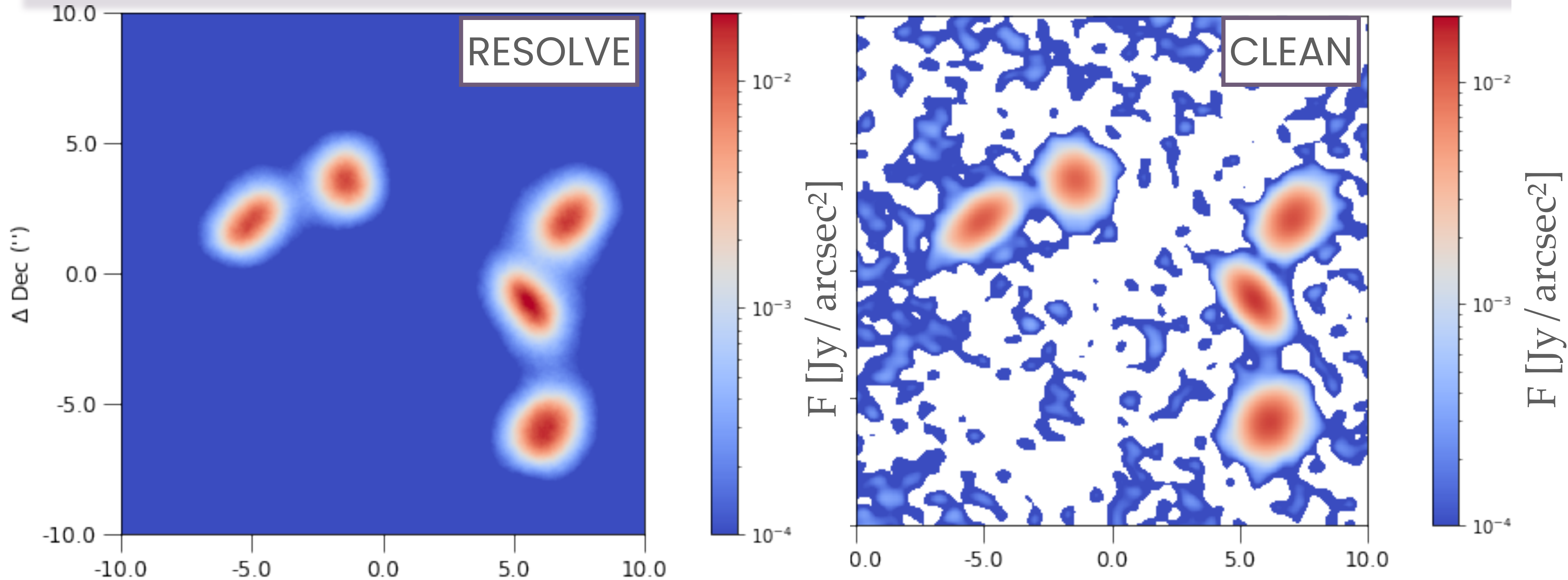


Final results of RESOLVE imaging



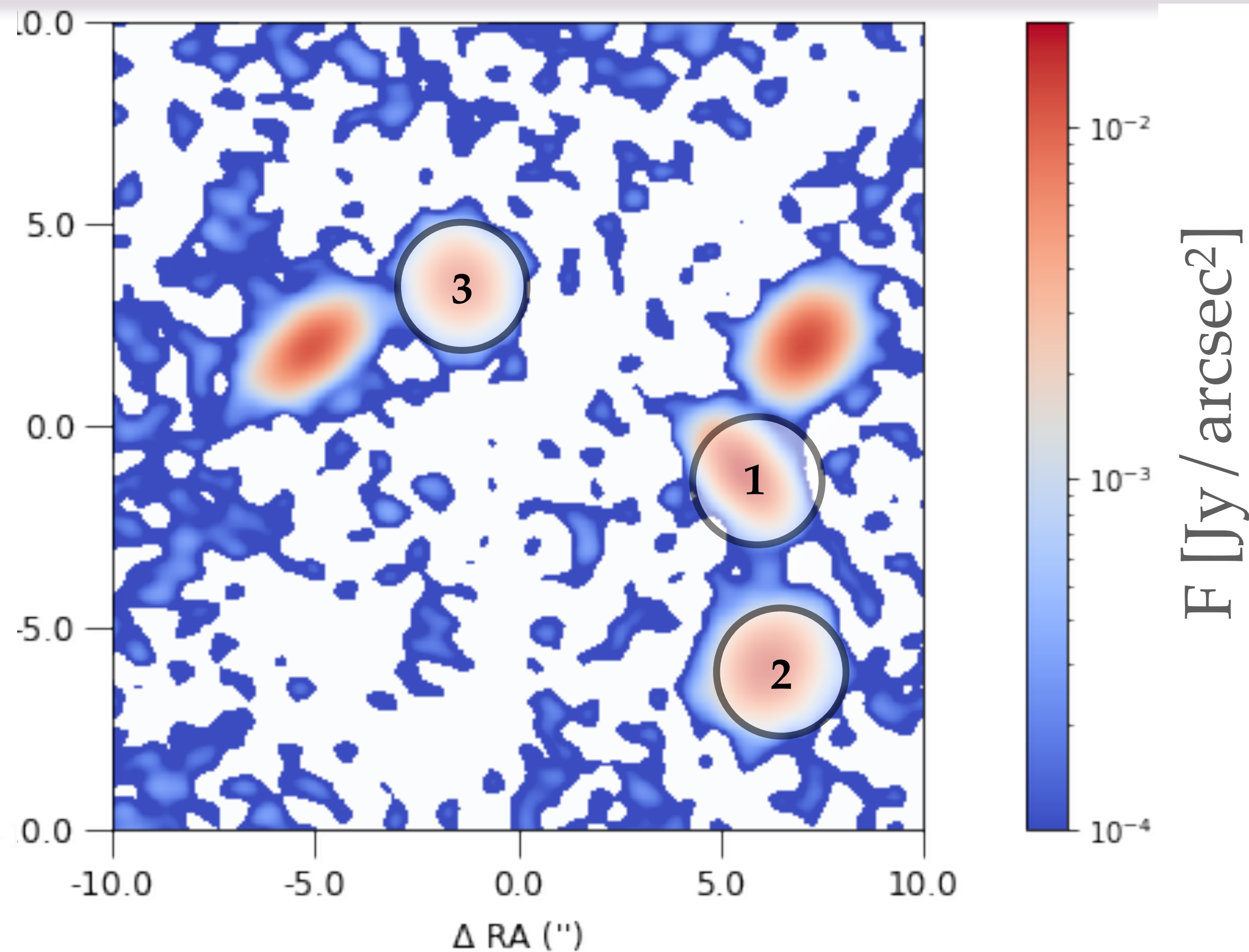
Five sources are recovered and uncertainty map is obtained

Direct comparison of imaging for simulated datasets



Note only positive emission in RESOLVE image

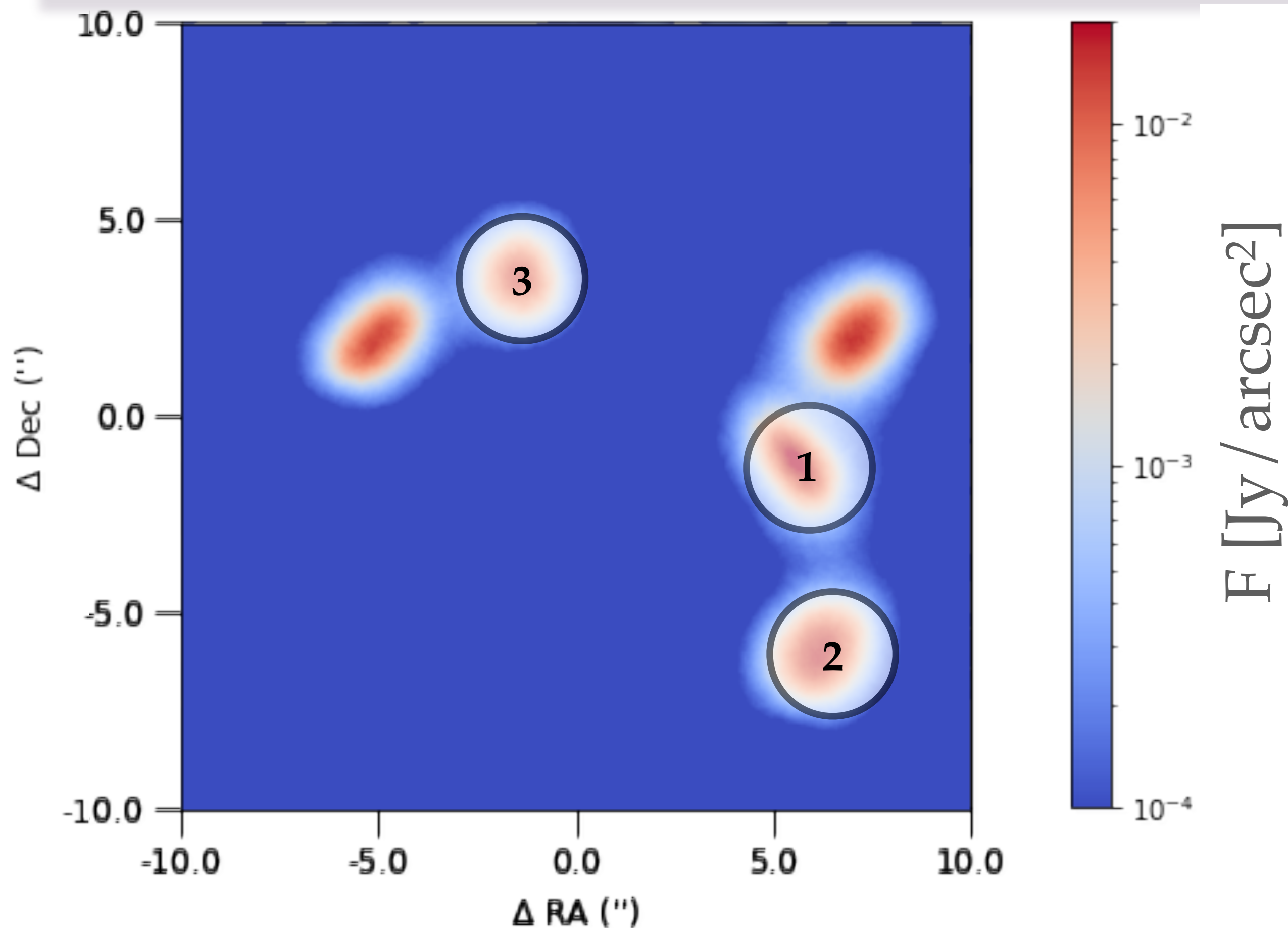
Recovery of flux by CLEAN and RESOLVE



Source	CLEAN Flux [mJy]	RESOLVE Flux [mJy]	Model Flux [mJy]
1	24.96	26.68	34.11
2	23.59	23.59	23.31
3	17.82	17.82	16.69

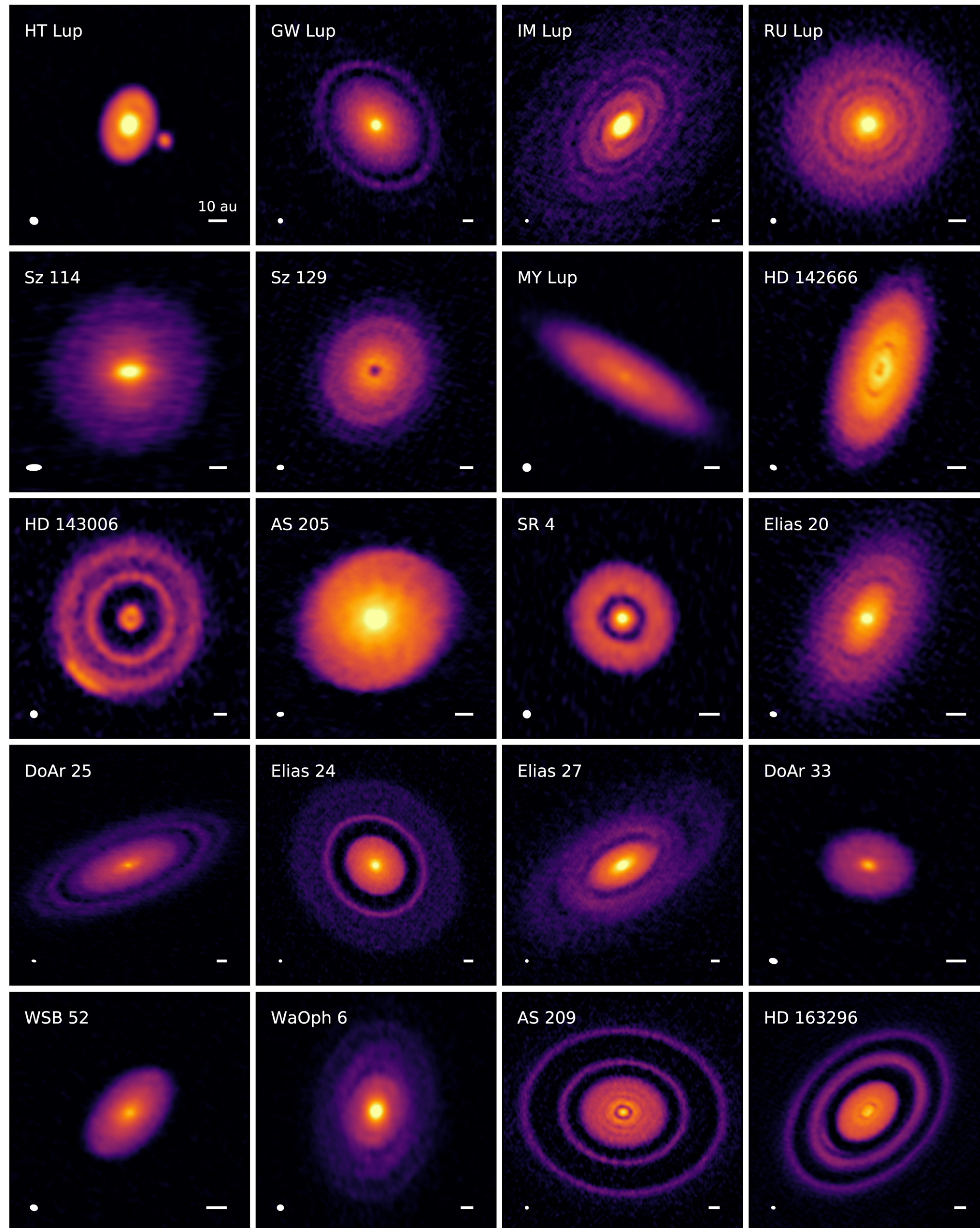
Comparable fluxes retrieved by CLEAN and RESOLVE

Recovery of flux by CLEAN and RESOLVE



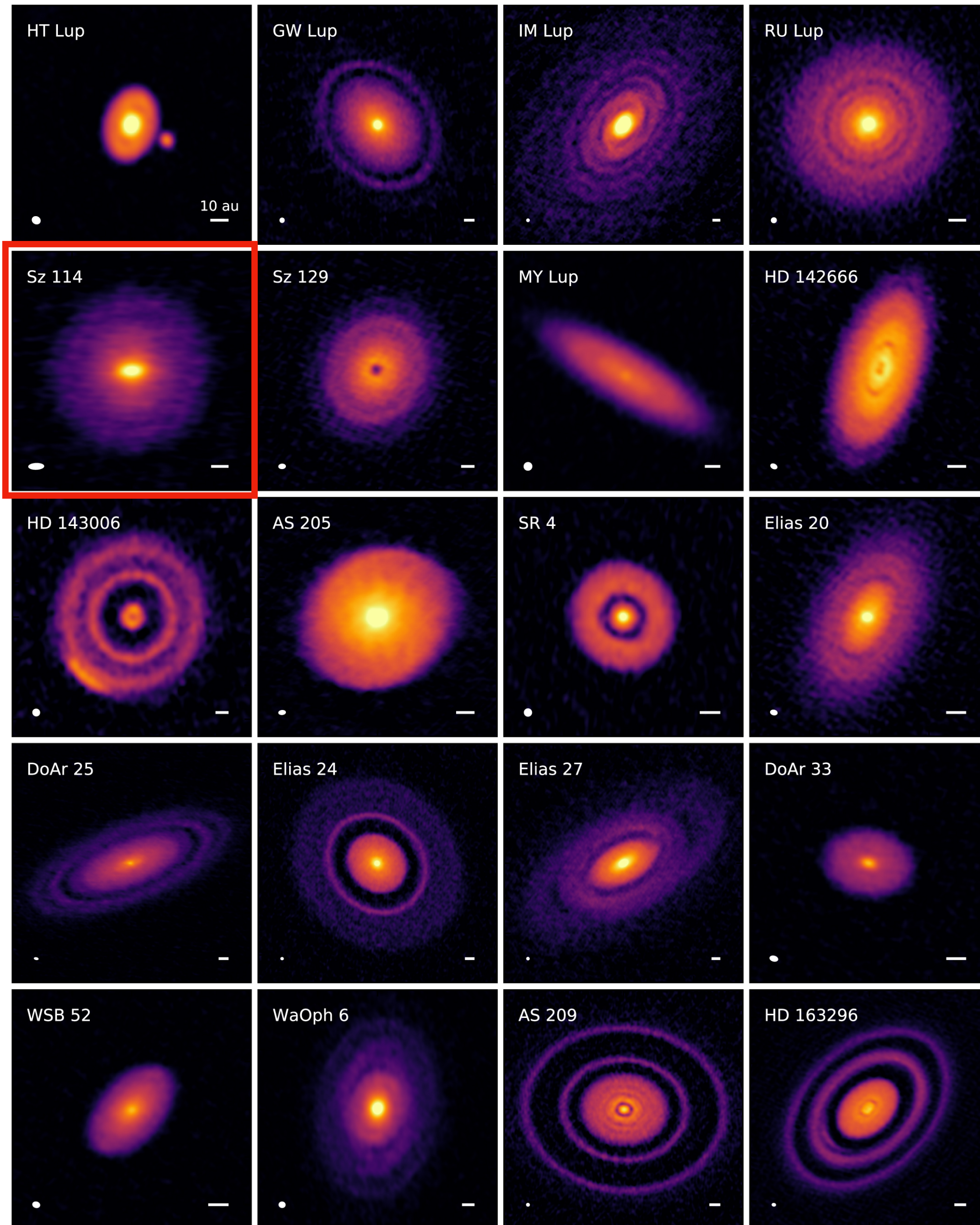
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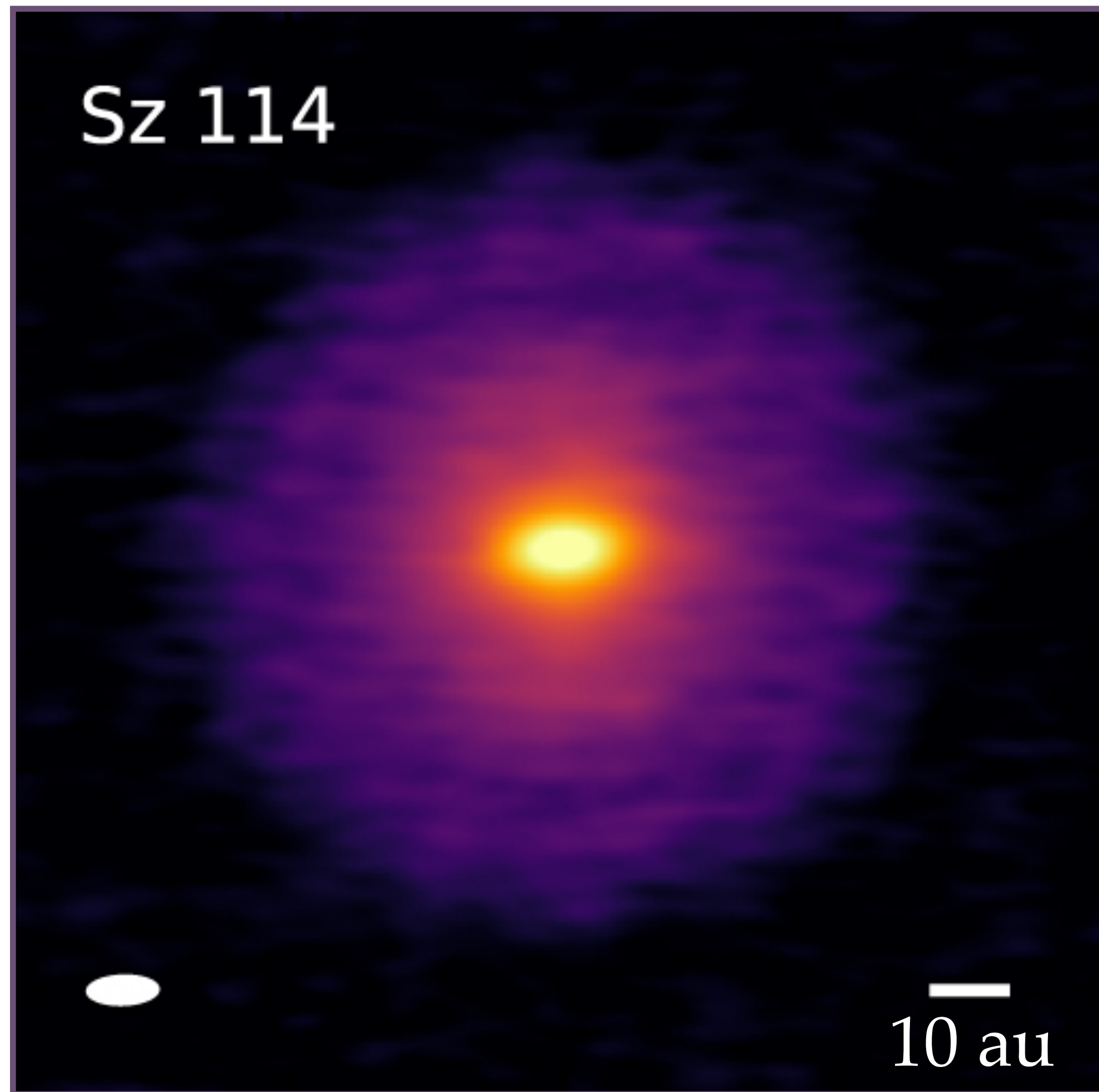
RESOLVE application to real data

Dust emission from planet-forming disk



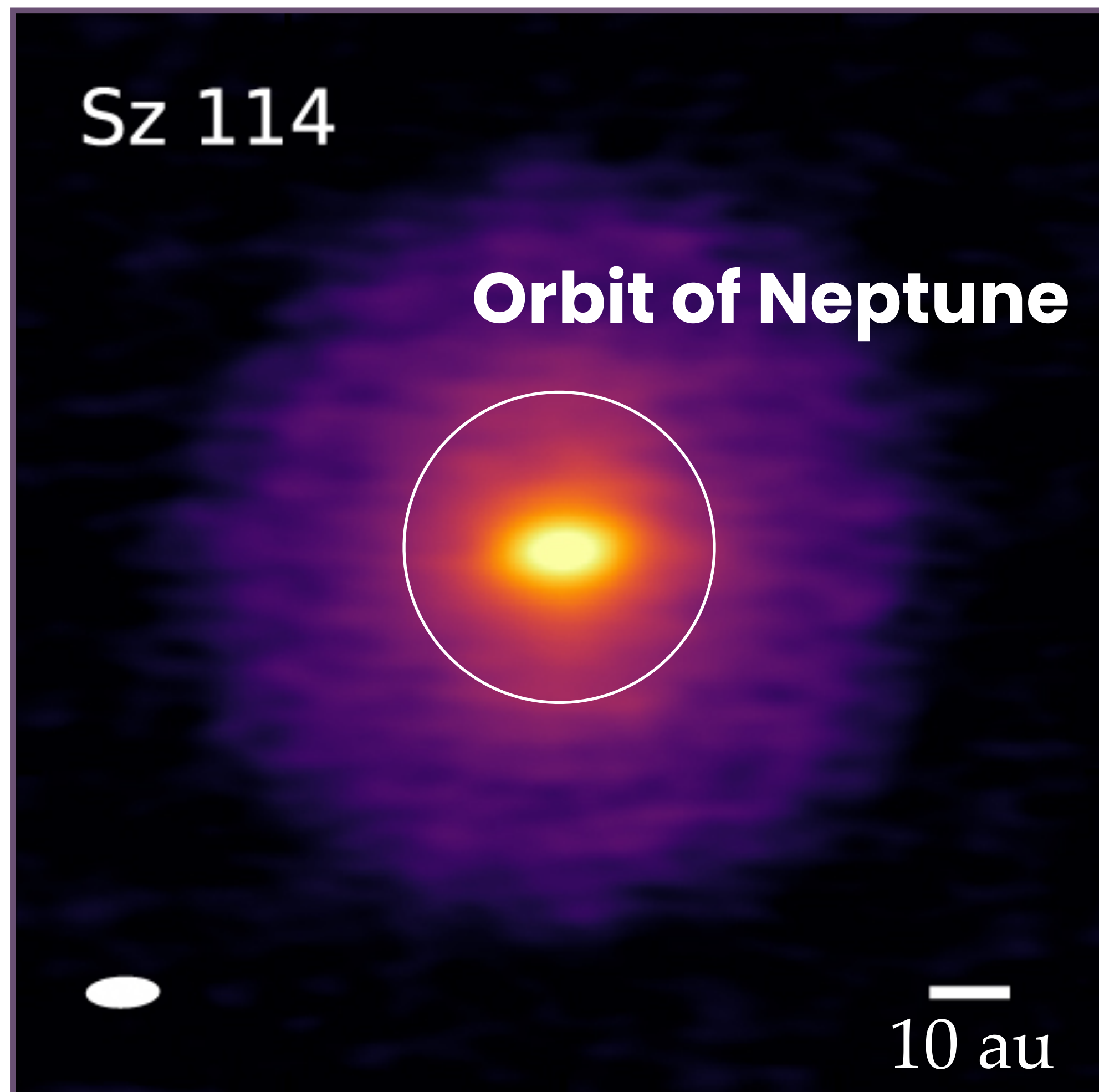
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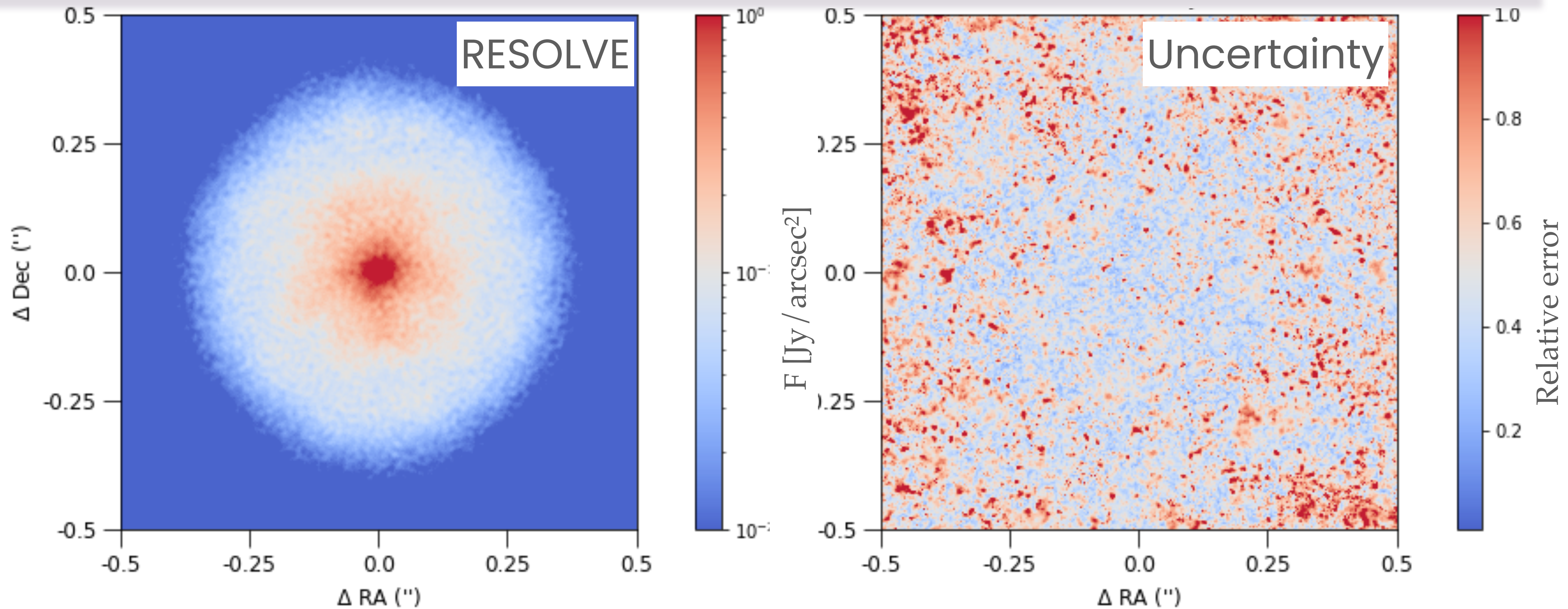
Dust emission from planet-forming disk



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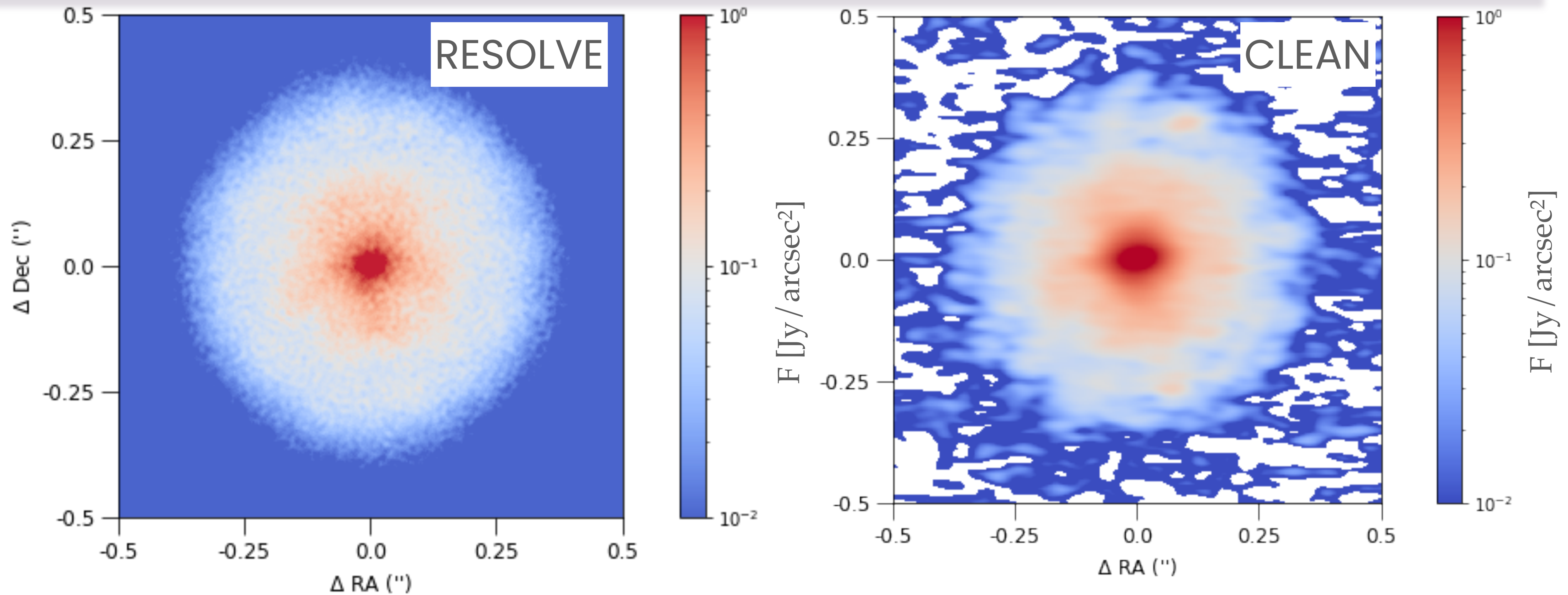
Dust emission from planet-forming disk

Final image and uncertainty for Sz114 disk



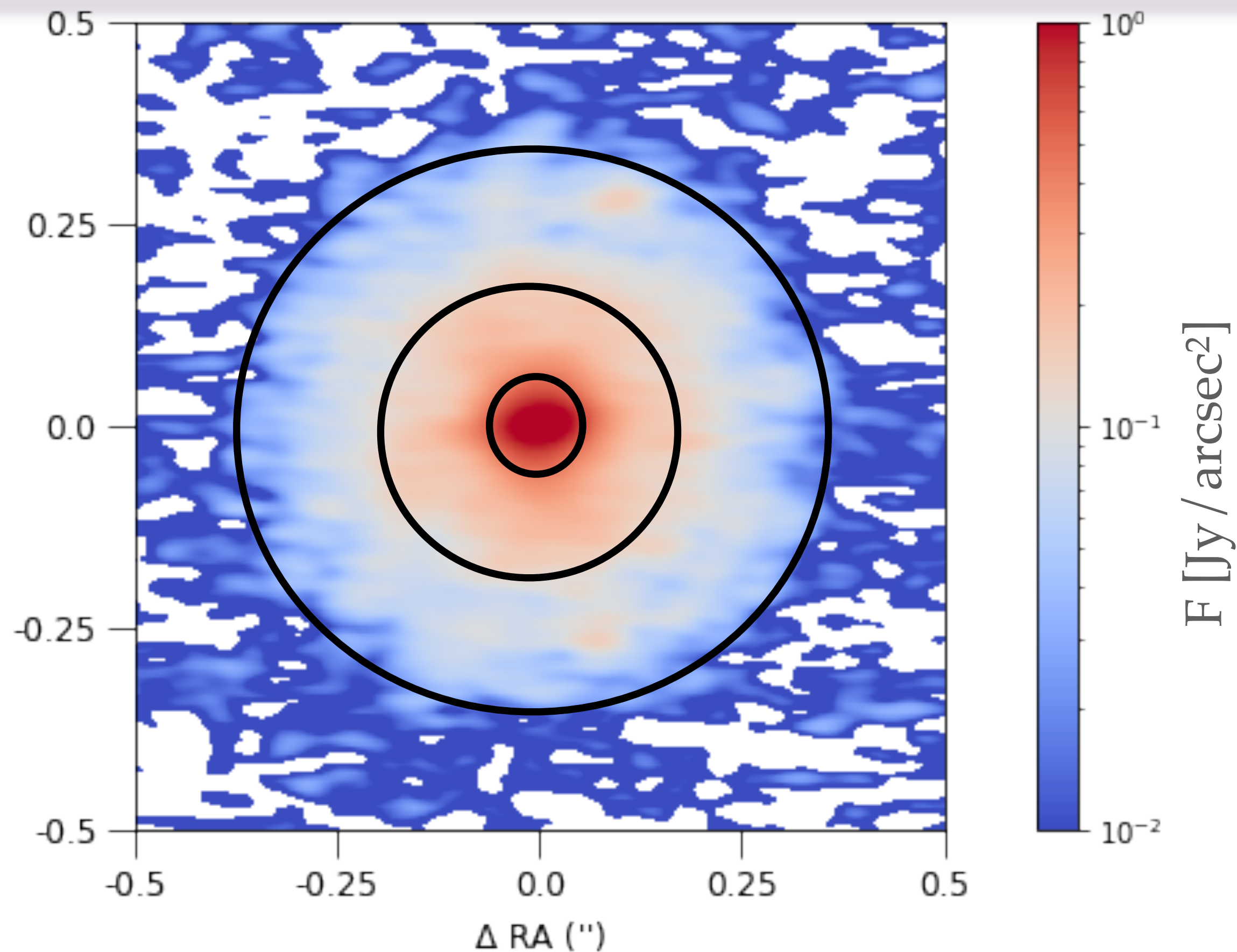
High-quality map of dust in protoplanetary disk obtained by RESOLVE

Direct comparison of results for Sz 114 protoplanetary disk



RESOLVE reveals potential for 'super-resolution'

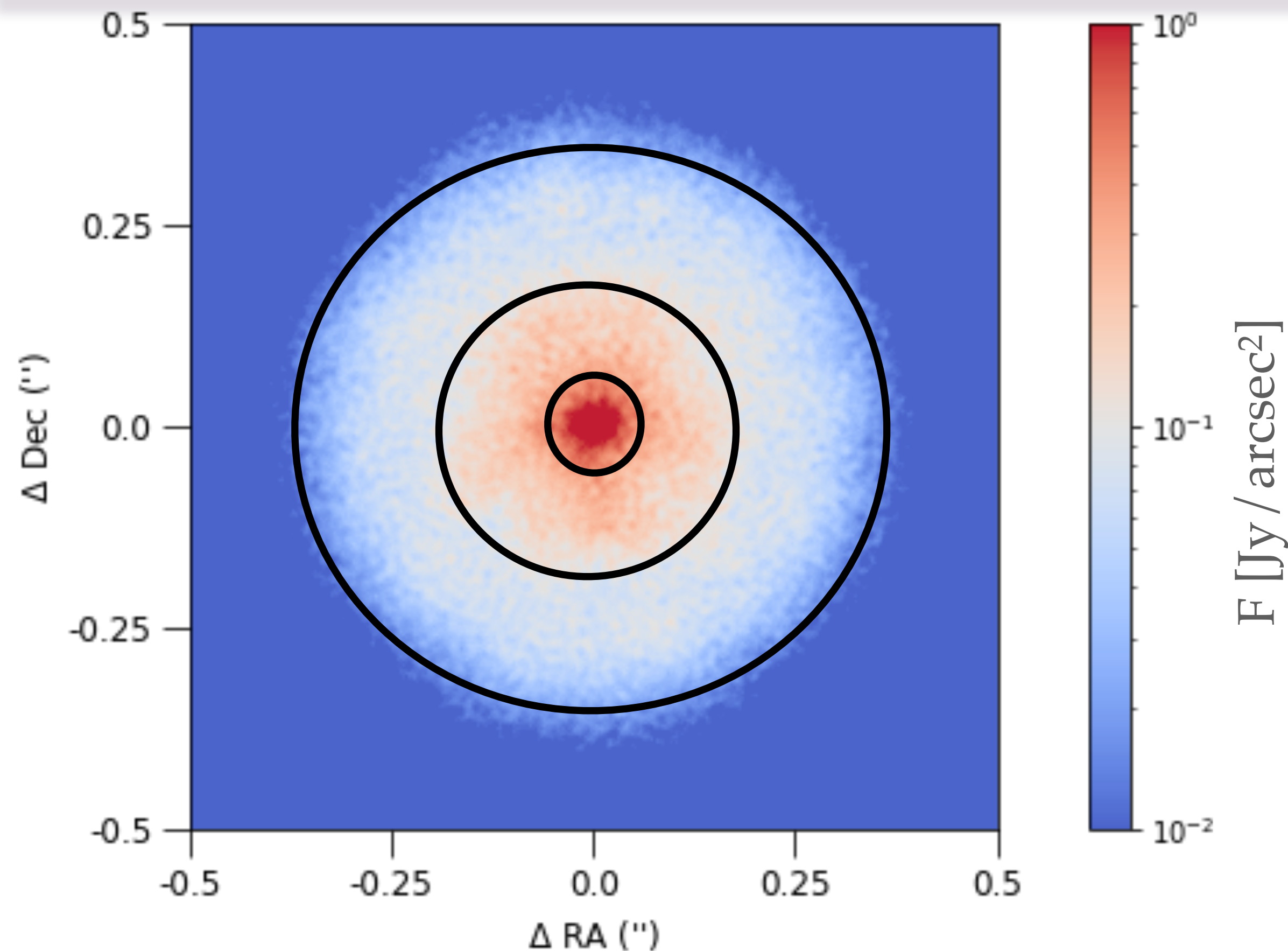
Flux comparison of results for Sz 114 protoplanetary disk



r	CLEAN Flux [mJy]	RESOLVE Flux [mJy]	CLEAN/RESOLVE
0.06"	8.95	9.48	95 %
0.15"	22.53	23.21	97 %
0.35"	47.24	47.24	100 %

Comparable fluxes retrieved by CLEAN and RESOLVE

Flux comparison of results for Sz 114 protoplanetary disk



r	CLEAN Flux [mJy]	RESOLVE Flux [mJy]	CLEAN/RESOLVE
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Comparable fluxes retrieved by CLEAN and RESOLVE

Conclusions



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Conclusions

- ✓ We successfully applied RESOLVE algorithm to ALMA data
- ✓ RESOLVE recovers flux with comparable accuracy to CLEAN in simulated data and real ALMA observations
- ✓ We achieve super-resolution image of planet-forming disk with RESOLVE along with uncertainty map
- ✓ RESOLVE presents a potential to push forward imaging procedures of interferometric observations and enhance / support capabilities of CLEAN